

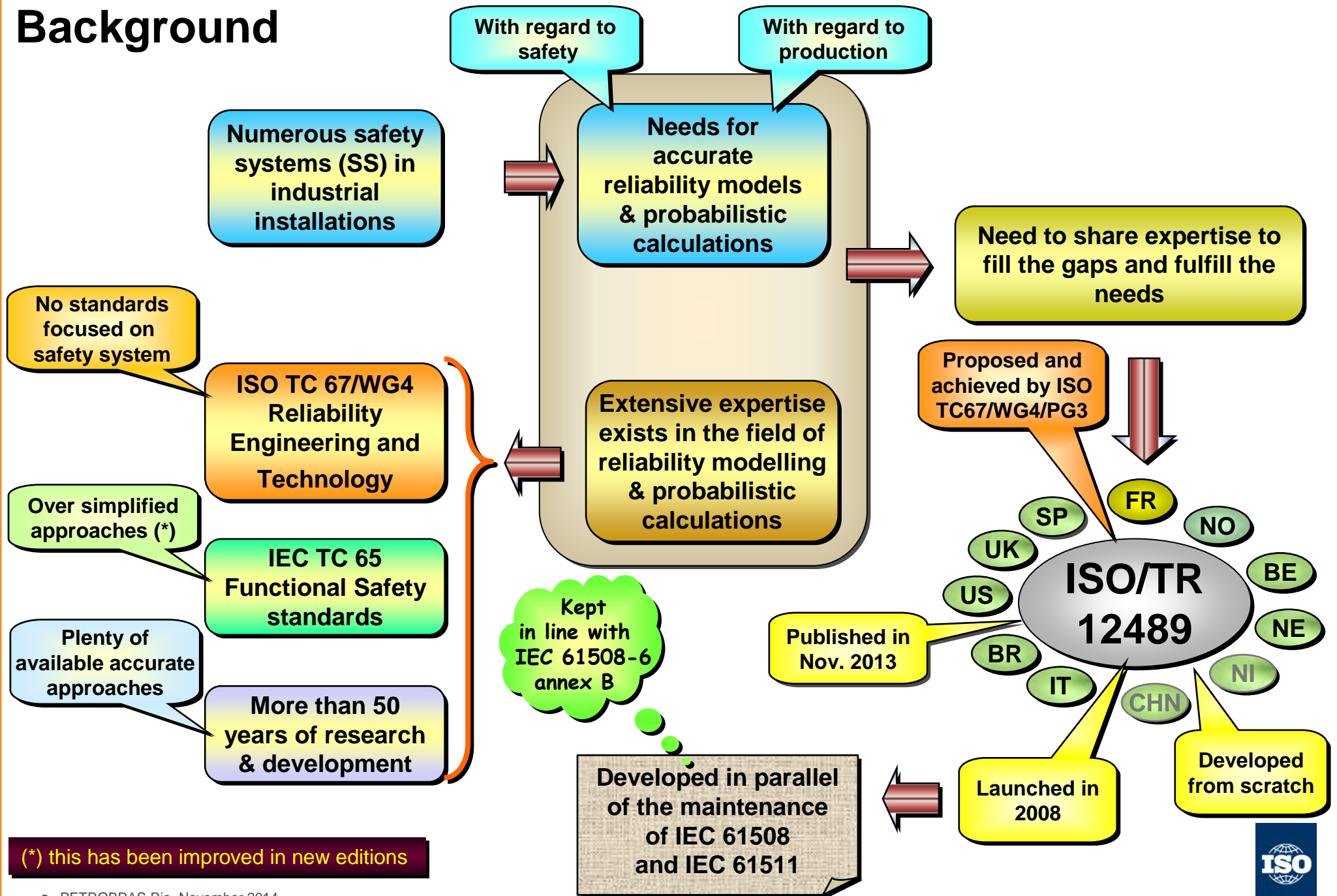
ISO/TR 12489: Reliability modelling & calculation of safety systems. Presentation and applications

Jean-Pierre SIGNORET
ISO/TR 12489 project leader
Reliability expert, TOTAL

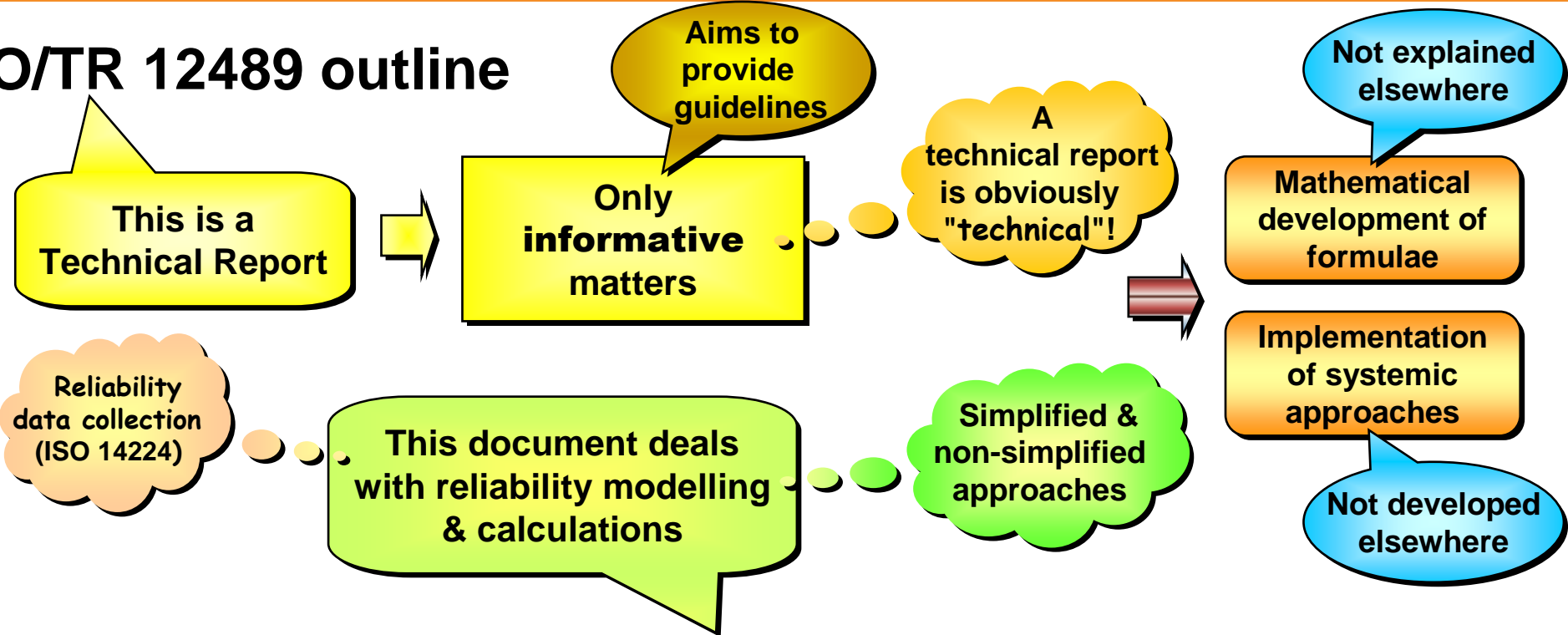
Presentation of ISO/TR 12489

TR prepared by ISO TC67 WG4/Project Group 3
PG3 leader : Jean Pierre Signoret (Total)
WG4 Convenor: Runar Østebø (Statoil)

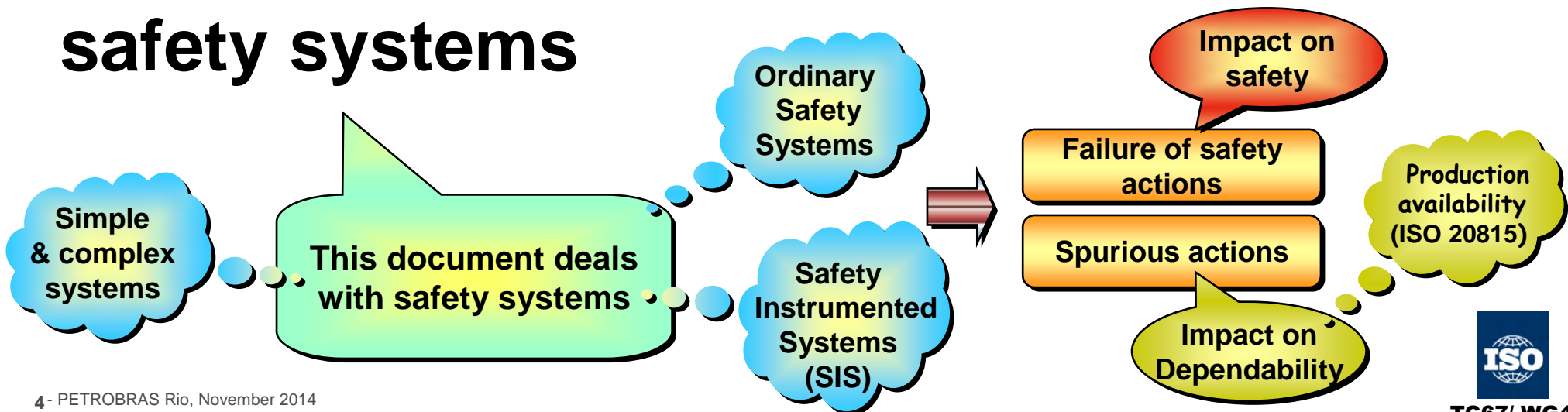
Background



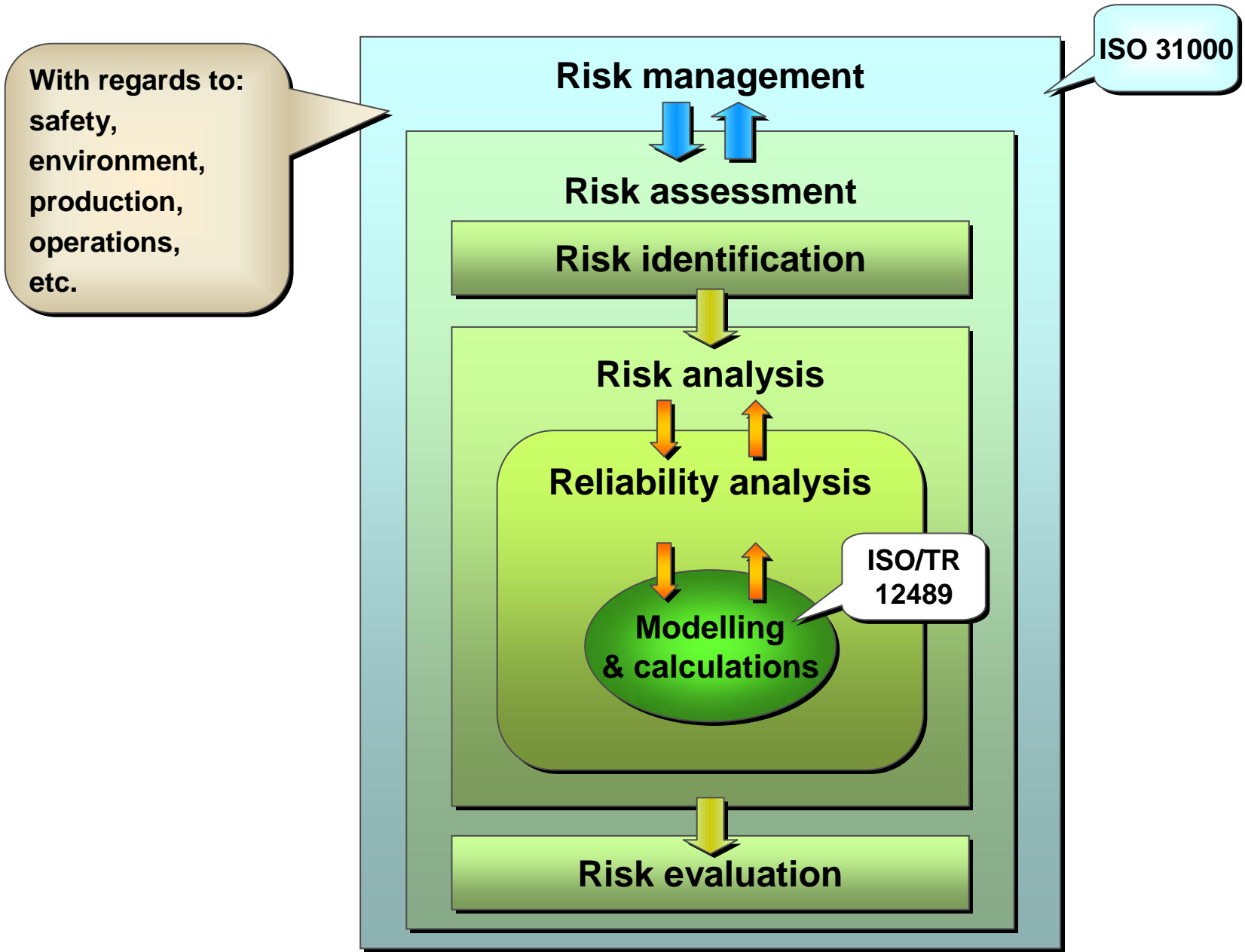
ISO/TR 12489 outline



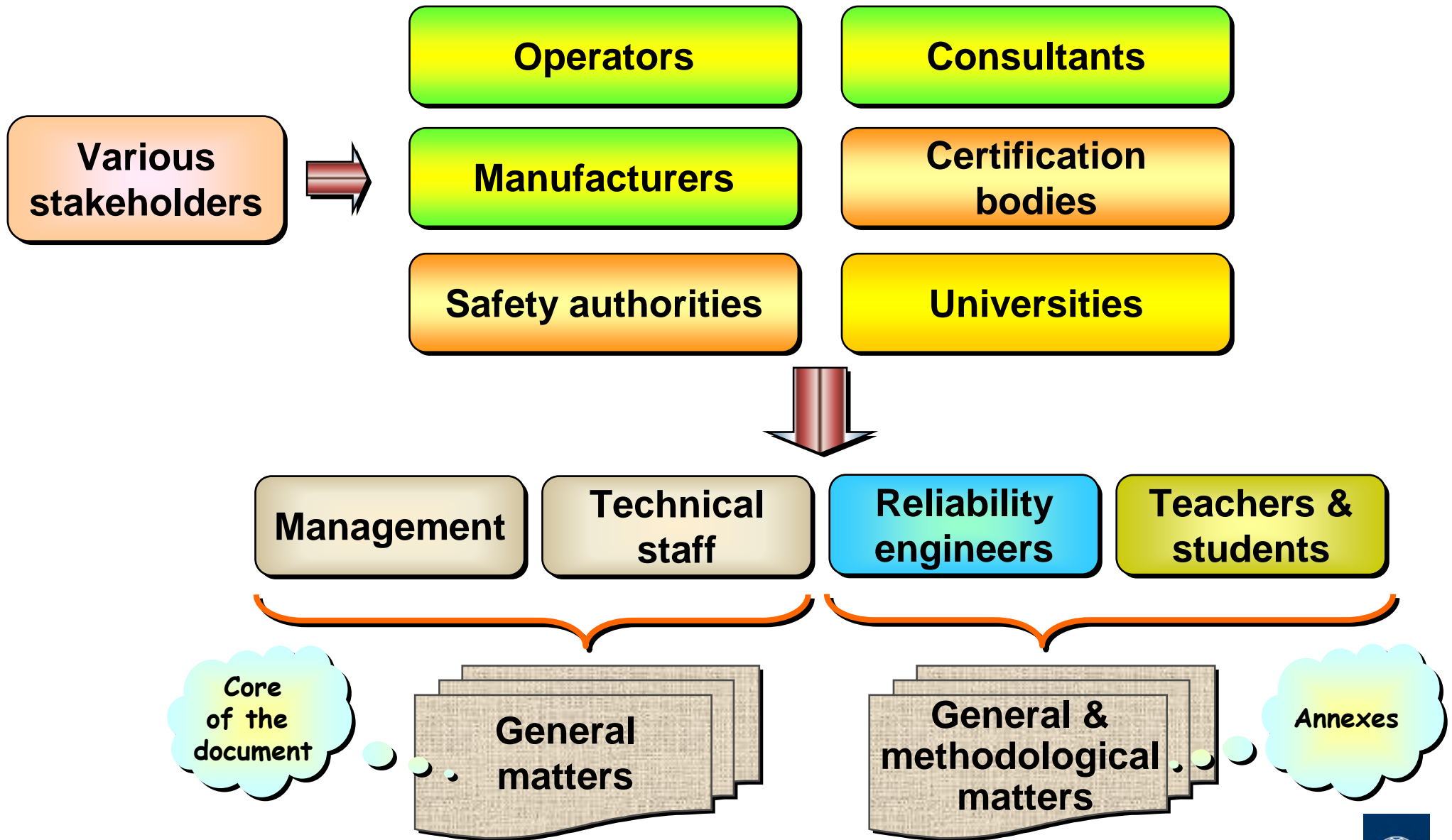
Reliability modelling & calculation of safety systems



Overall framework of ISO/TR 12489

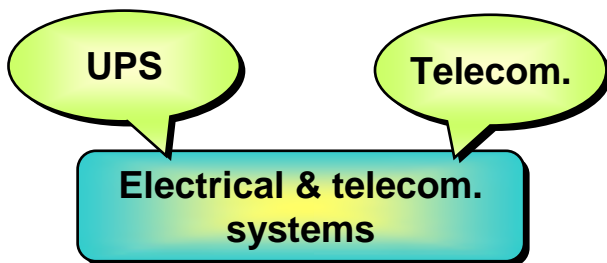
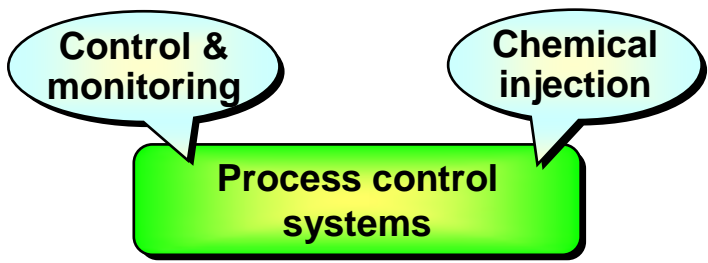
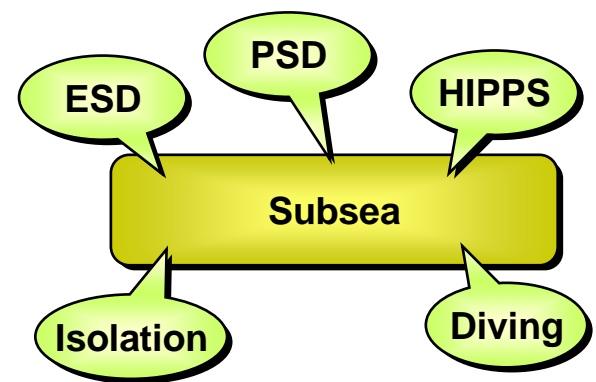
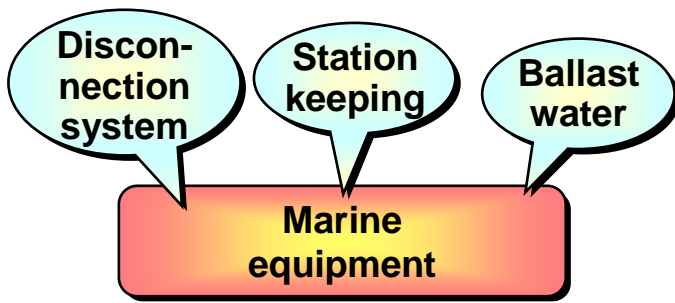
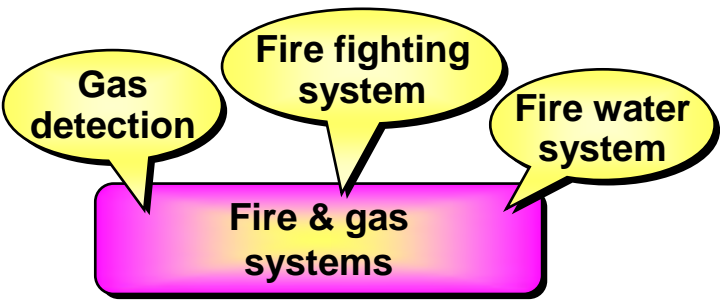
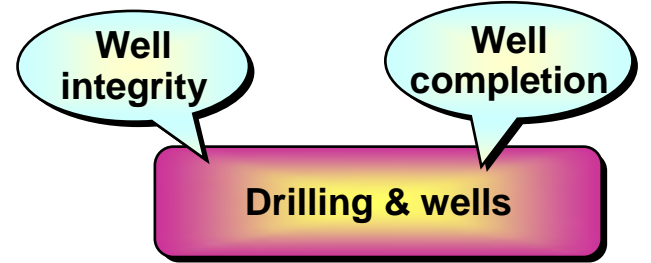
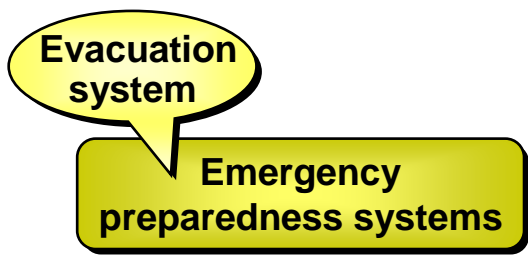
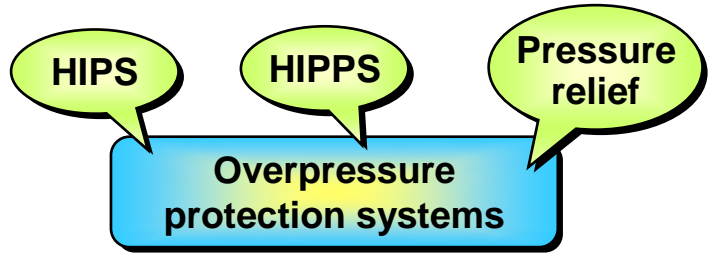
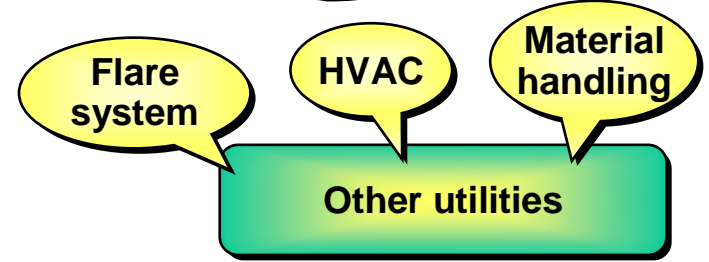
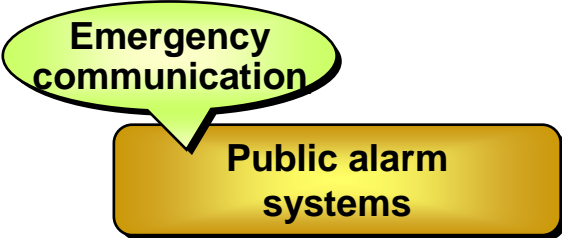
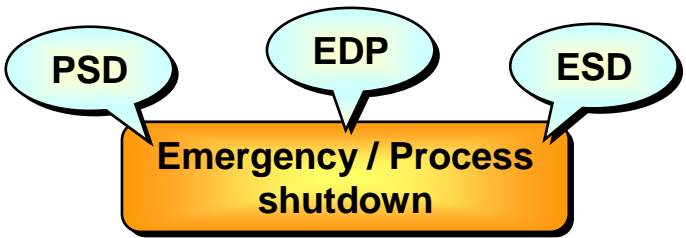


Target users of ISO/TR 12489

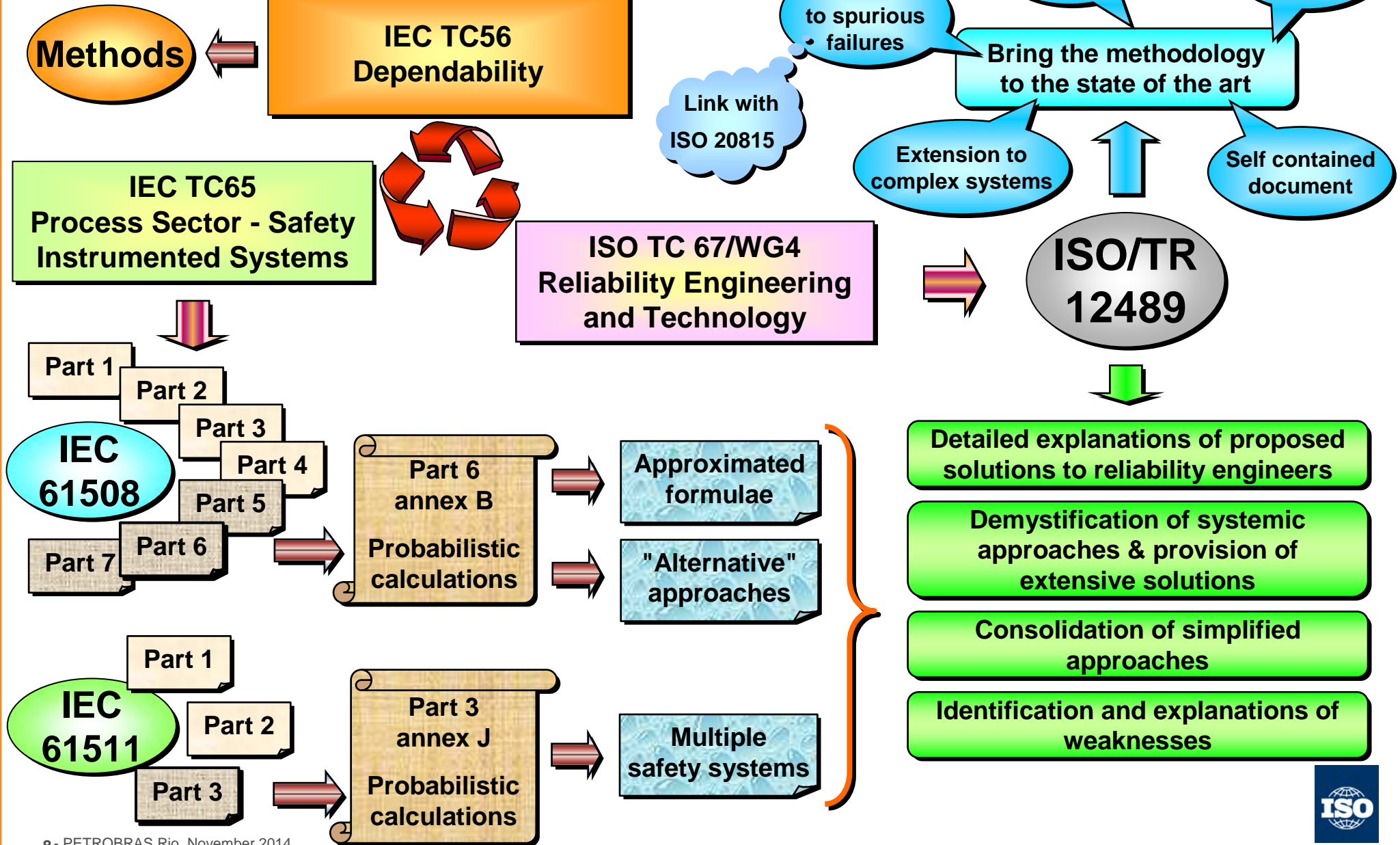


Some examples of safety systems covered by ISO/TR 12489 (instrumented or not)

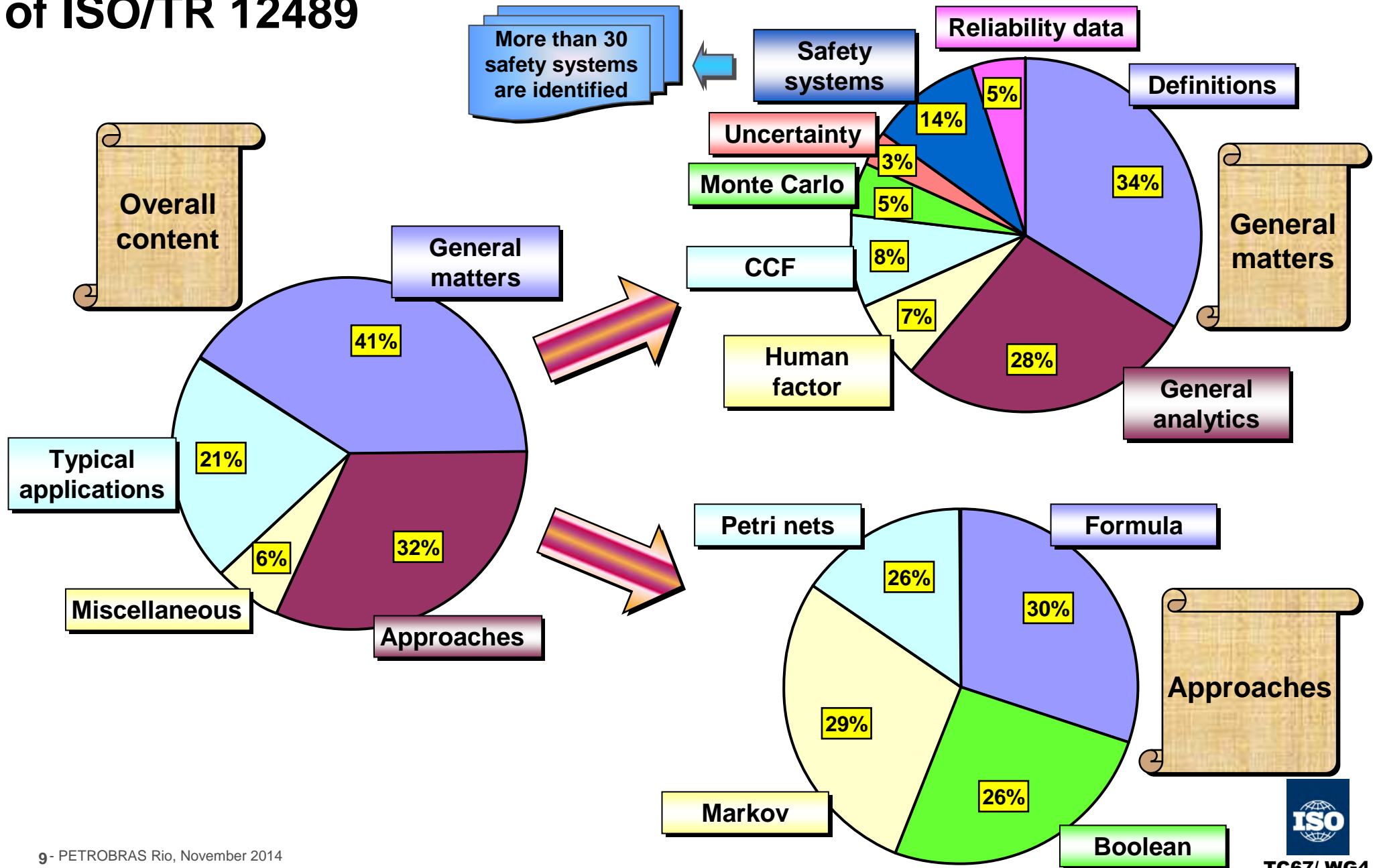
31 systems identified in the TR



ISO/TR 12489 versus IEC 61508/511 and IEC TC56



Distribution of the topics within the 260 pages of ISO/TR 12489



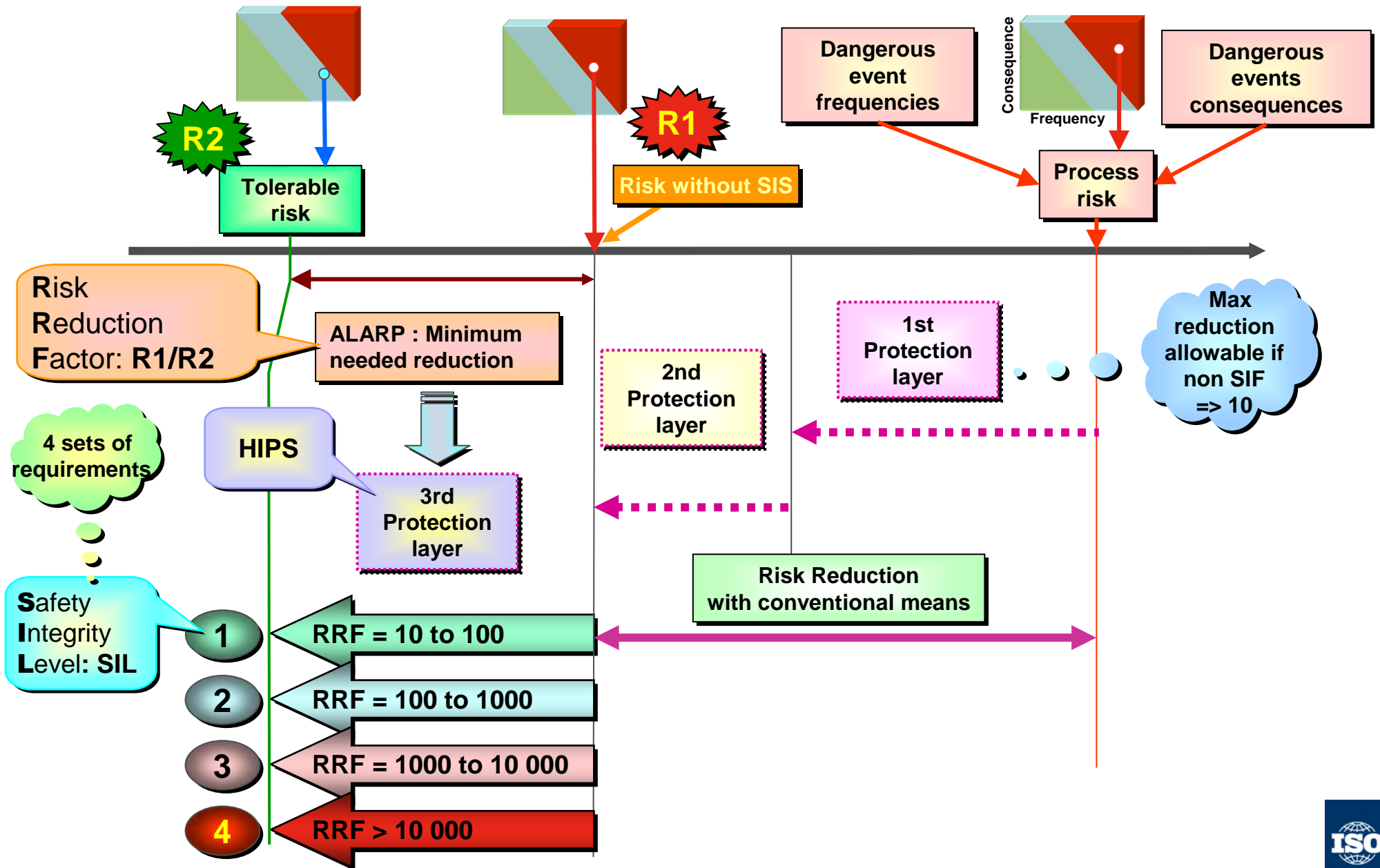
Introduction to functional safety concepts

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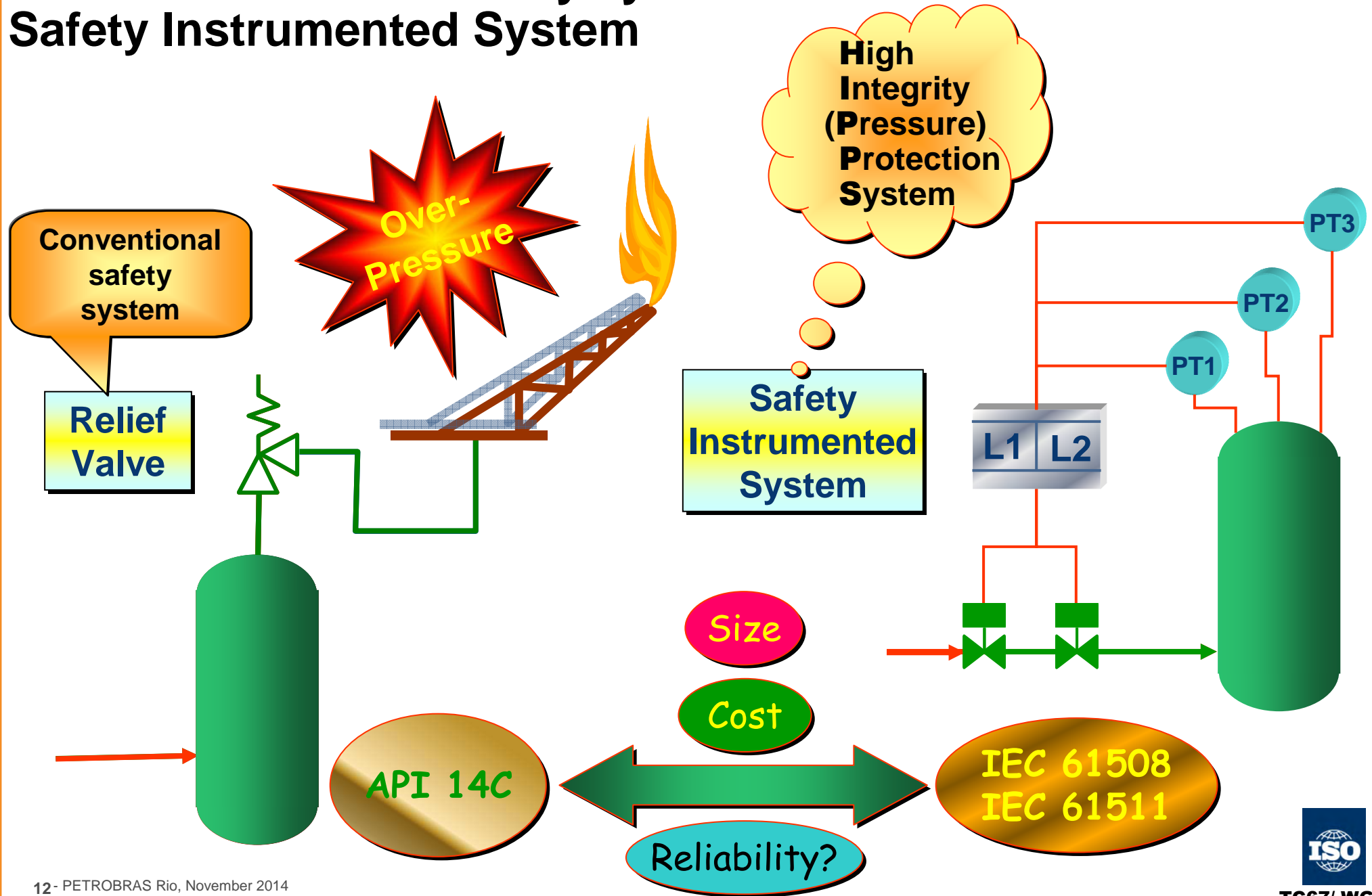
TC67
WG4



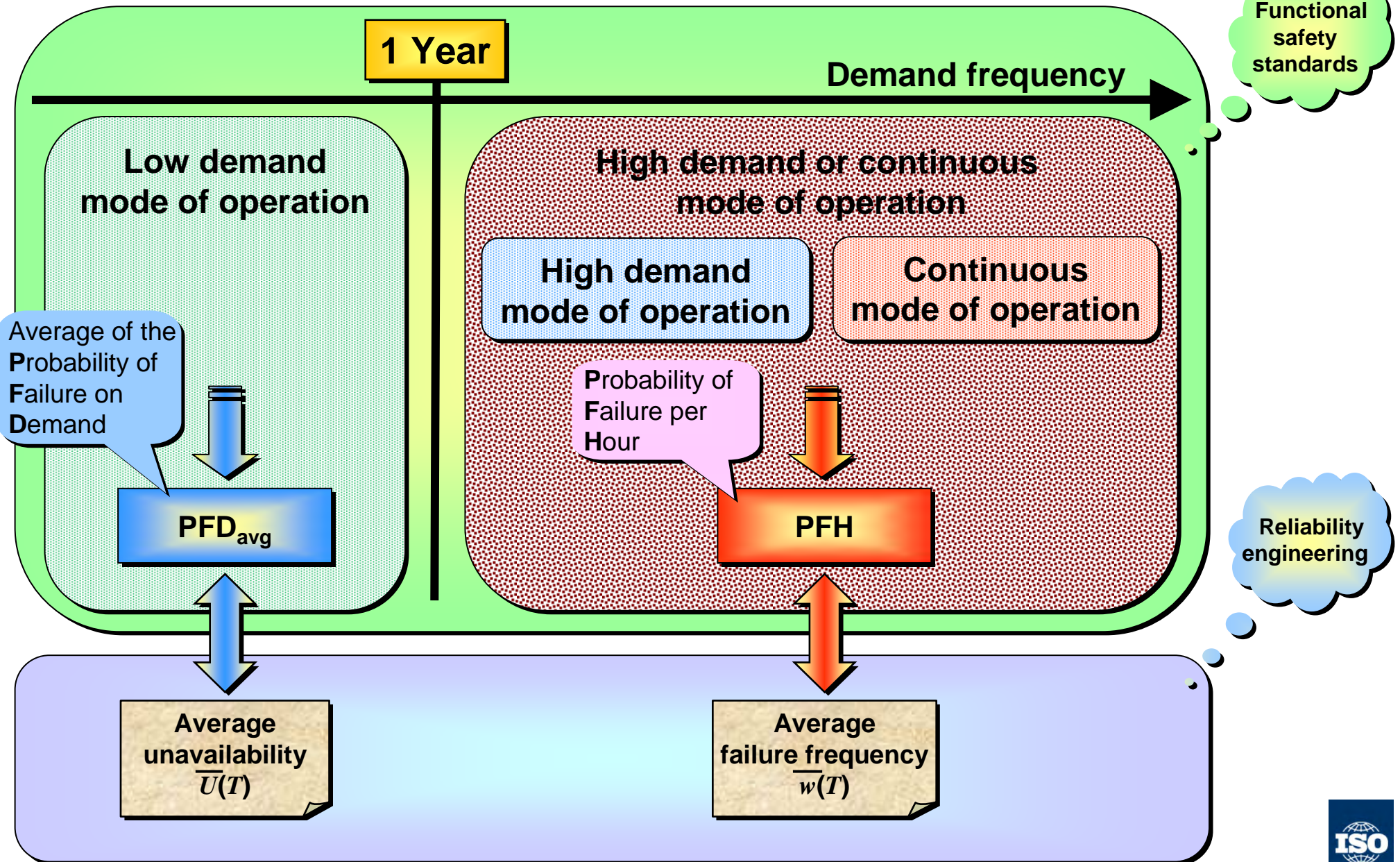
SIL Principle: identification of *Risk Reduction* needed



From conventional Safety system to Safety Instrumented System

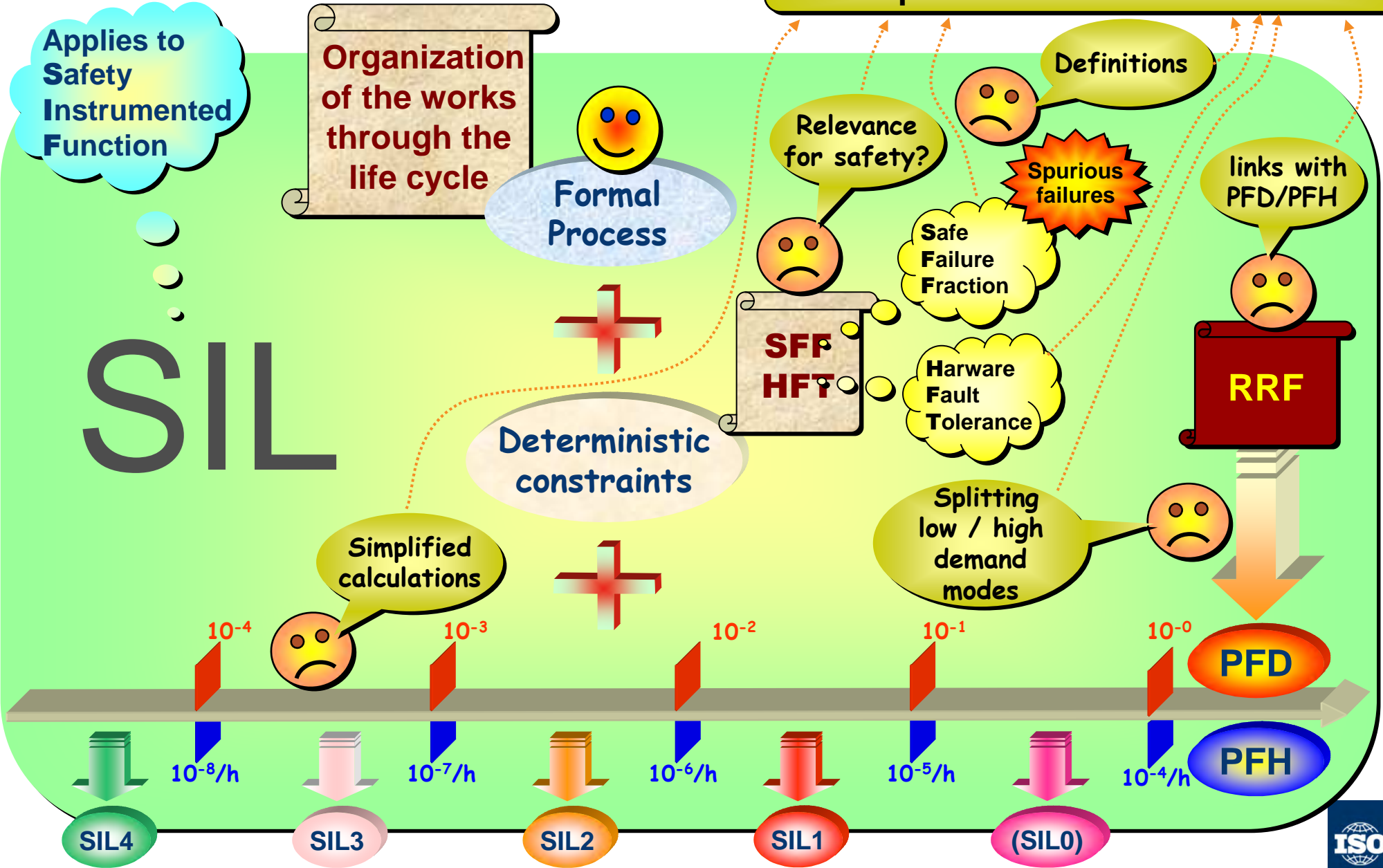


Types of Safety Instrumented Systems (SIS)

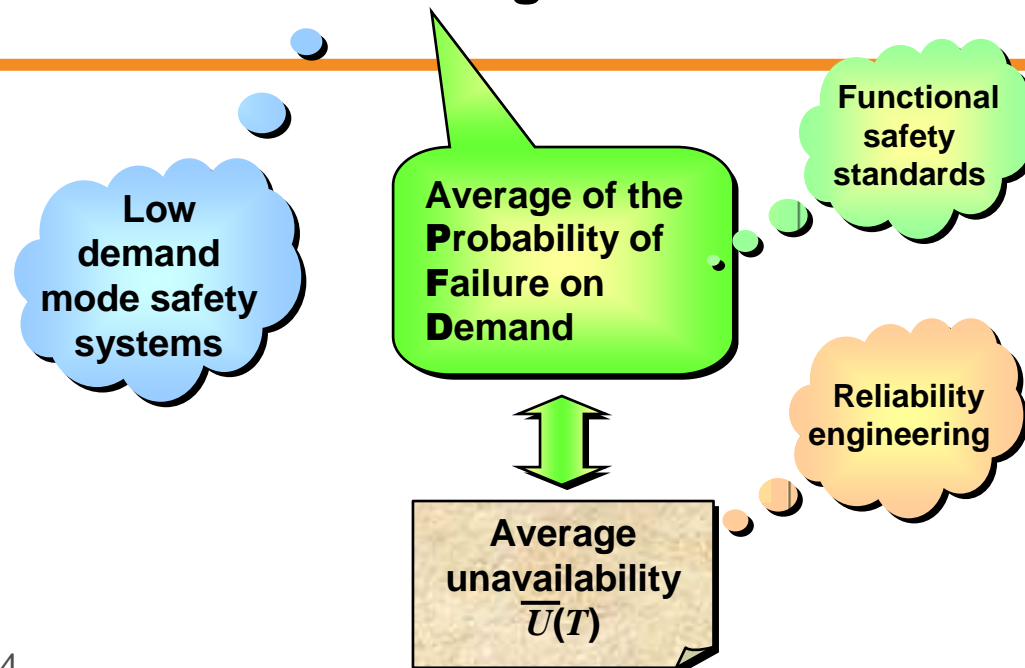


SIL- summary & difficulties

Proposed clarifications, explanations & improvements in ISO/TR 12489

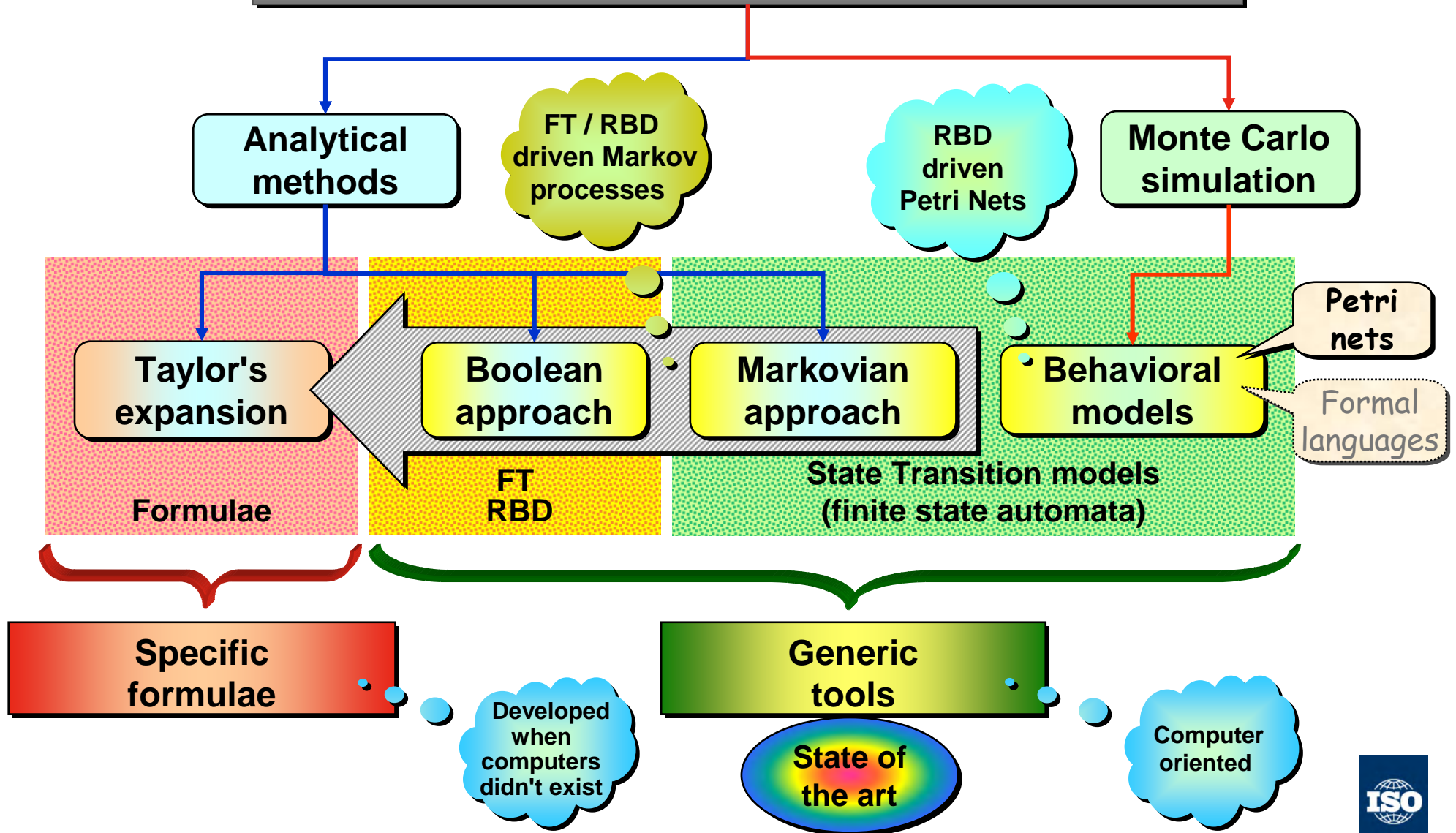


Introduction to the methods developed into ISO/TR 12489 for PFD_{avg} calculations



50 years of experience

Probabilistic models overview



Simplified analytical approach

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Simplest approximation of the PFDavg

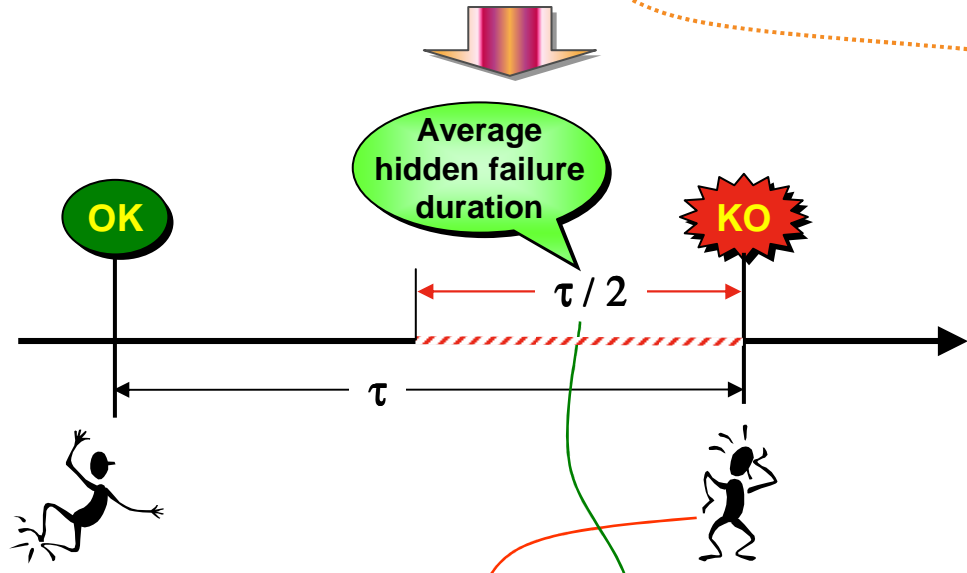


$$\tau \ll 1/\lambda$$

2 parameters:
 λ : Failure rate
 τ : test interval

$$U(\delta) = 1 - \exp(-\lambda\delta) \approx \lambda\delta$$

$$PFD_{avg} = \bar{U}(\tau) \approx \frac{1}{\tau} \int_0^\tau \lambda\delta \cdot d\delta = \frac{1}{\tau} \frac{\lambda\tau^2}{2} = \frac{\lambda\tau}{2}$$



Not realistic!

$$\lim_{\tau \rightarrow 0} PFD_{avg} = 0$$

But

Unavailability duration δ_{unv}

Proba. of hidden failures $\lambda \cdot \frac{\tau}{2}$

$$\delta_{unv} \approx \lambda\tau \cdot \frac{\tau}{2}$$

$$PFD_{avg} \approx \frac{\delta_{unv}}{\tau} = \frac{\lambda\tau}{2}$$

The most famous formula in functional safety

Approximation of the PFDavg from IEC 61508

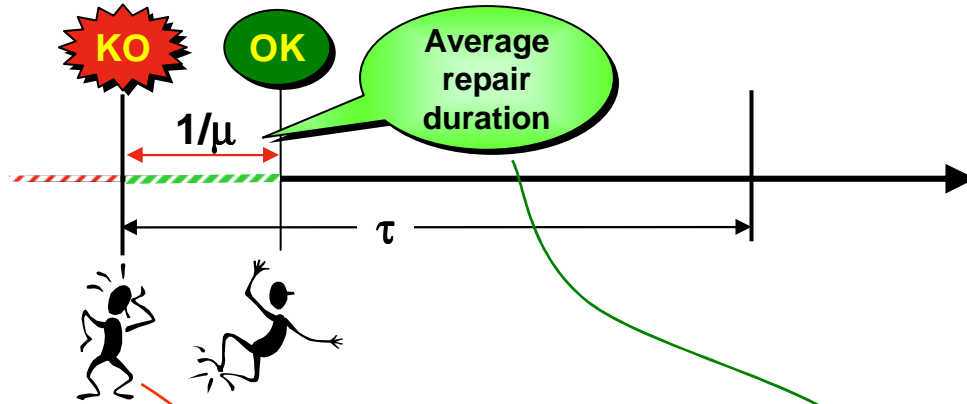


Diagram of a component A. A yellow box lists three parameters:

- λ : Failure rate
- τ : test interval
- μ : repair rate

Callouts show the conditions $\tau \ll 1/\lambda$ and $1/\mu \ll \tau$.

$$\tau - \frac{1}{\mu} \approx \tau$$

Unavailability duration

$$\delta_{unv} \approx \lambda\tau \cdot \frac{\tau}{2} + \lambda\tau \cdot \frac{1}{\mu}$$

Proba. of hidden failures

IEC 61508 formula

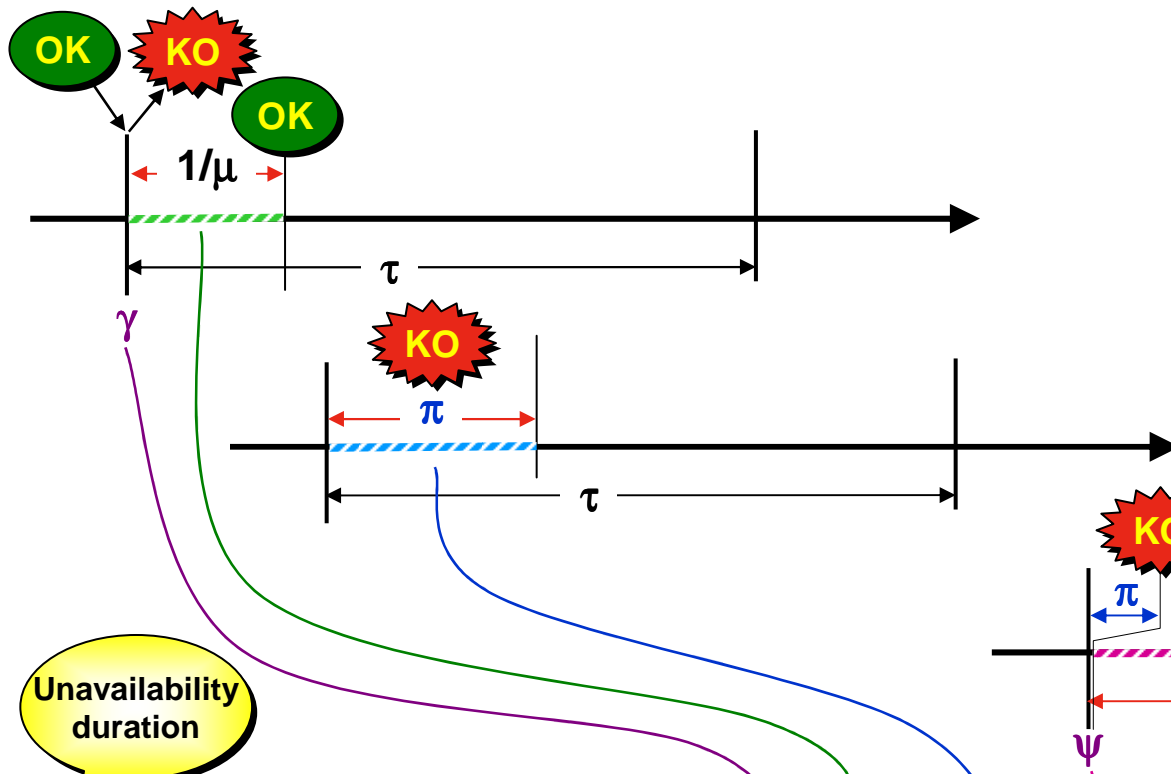
But

Influent parameters are missing

$$PFD_{avg} \approx \frac{\delta_{unv}}{\tau} = \frac{\lambda\tau}{2} + \frac{\lambda}{\mu}$$

\bar{u}
of revealed failures

Approximation of the PFDavg with more parameters (ISO/TR 12489)



- Parameters:**
- λ : failure rate
 - τ : test interval
 - μ : repair rate
 - γ : prob. failure due to a demand
 - π : test duration
 - ψ : reconfiguration error

- $\tau \ll 1/\lambda$
- $1/\mu \ll \tau$
- $\pi \ll \tau$

$$\tau - \pi \approx \tau$$

$$\delta_{unv} \approx \lambda\tau \cdot \frac{\tau}{2} + \lambda\tau \frac{1}{\mu} + \gamma \cdot \frac{1}{\mu} + \pi + \psi \cdot \tau$$

$$PFD_{avg} \approx \frac{\delta_{unv}}{\tau} = \frac{\lambda\tau}{2} + \frac{\lambda}{\mu} + \frac{\gamma}{\mu \cdot \tau} + \frac{\pi}{\tau} + \psi$$

etc.

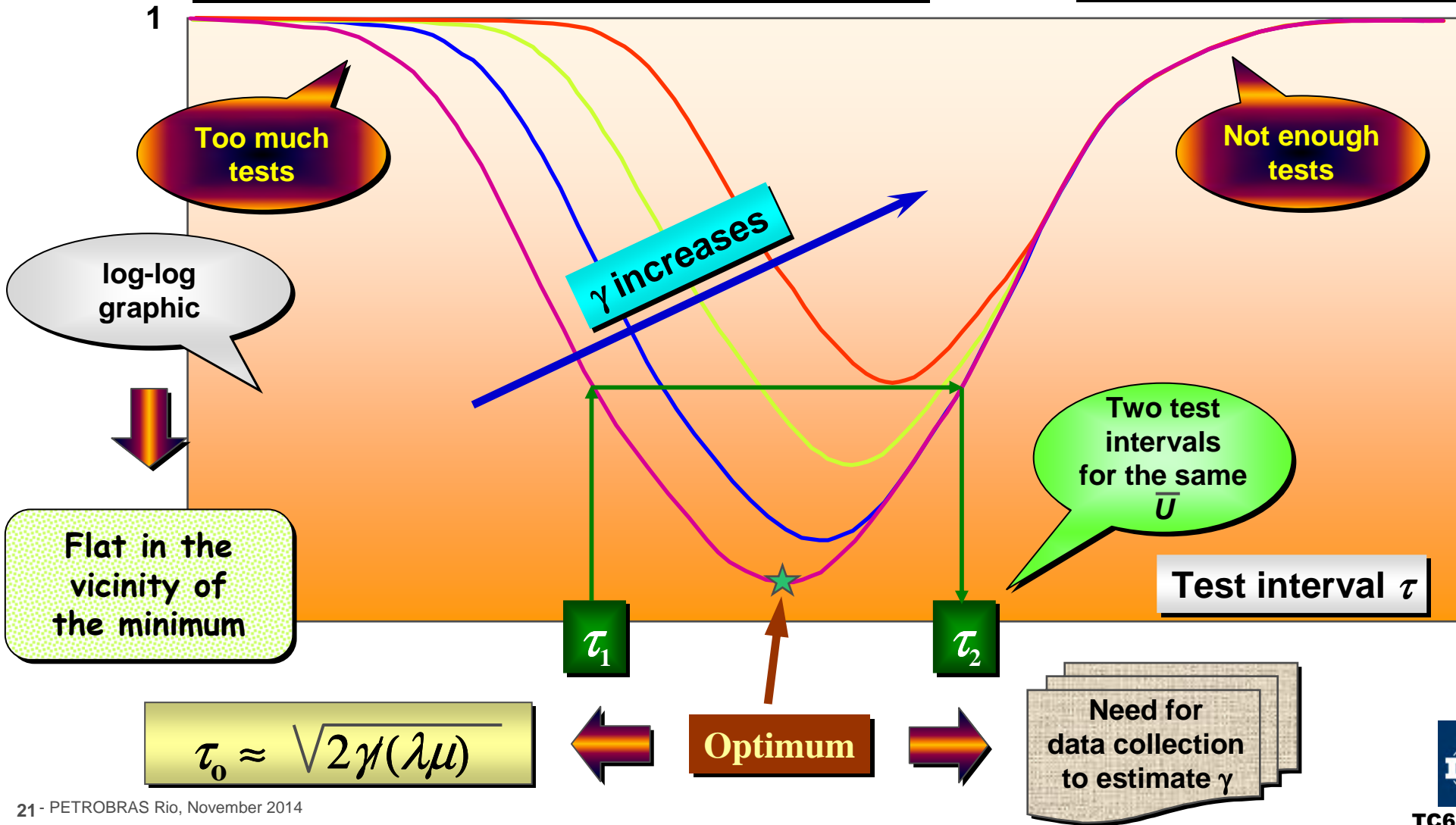
Taylor expansion for more complex cases

Limit average unavailability versus test interval



Parameters:
 λ : failure rate
 τ : test interval
 μ : repair rate
 γ : prob. failure due to a demand

Average unavailability $\bar{U} \equiv \text{PFD}_{\text{avg}}$



Flat in the vicinity of the minimum

$$\tau_0 \approx \sqrt{2\gamma(\lambda\mu)}$$

Optimum

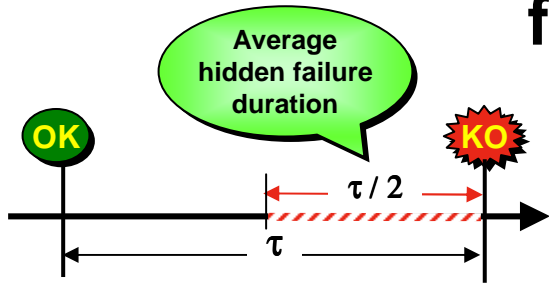
Need for data collection to estimate γ

Simplest approximation of the PFDavg for redundant systems

2 parameters:

λ : Failure rate
 τ : test interval

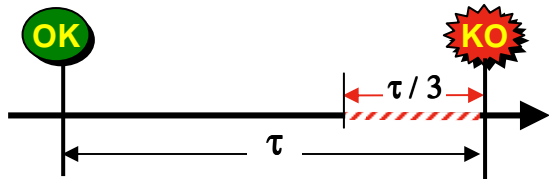
$$\tau \ll 1/\lambda$$



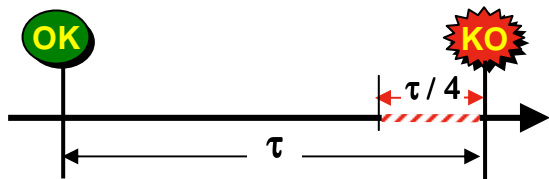
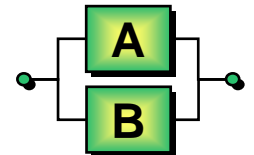
$$PFD_{avg} = \bar{U}_A(\tau) \approx \frac{1}{\tau} \int_0^{\tau} \lambda \cdot \delta \cdot d\delta = \frac{1}{\tau} \frac{\lambda \tau^2}{2} = \frac{\lambda \tau}{2}$$



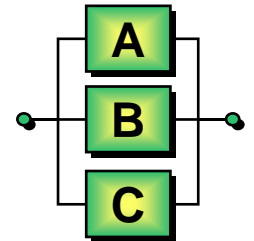
Taylor expansion
 $\lambda \delta \ll 1$



$$PFD_{avg} = \bar{U}_{AB}(\tau) \approx \frac{1}{\tau} \int_0^{\tau} (\lambda \cdot \delta)^2 d\delta = \frac{1}{\tau} \frac{\lambda^2 \tau^3}{3} = \frac{(\lambda \tau)^2}{3}$$



$$PFD_{avg} = \bar{U}_{ABC}(\tau) \approx \frac{1}{\tau} \int_0^{\tau} (\lambda \cdot \delta)^3 d\delta = \frac{1}{\tau} \frac{\lambda^3 \tau^4}{4} = \frac{(\lambda \tau)^3}{4}$$



Not possible to combine formulae!

Effect of systemic dependencies

$$\bar{U}_{AB}(\tau) \neq \bar{U}_A(\tau) \cdot \bar{U}_B(\tau), \quad \bar{U}_{ABC}(\tau) \neq \bar{U}_A(\tau) \cdot \bar{U}_B(\tau) \cdot \bar{U}_C(\tau)$$

Not in line with reliability analysis philosophy

Catalog of ad hoc formulae

Even for simplest systems, each case implies specific Taylor expansion development

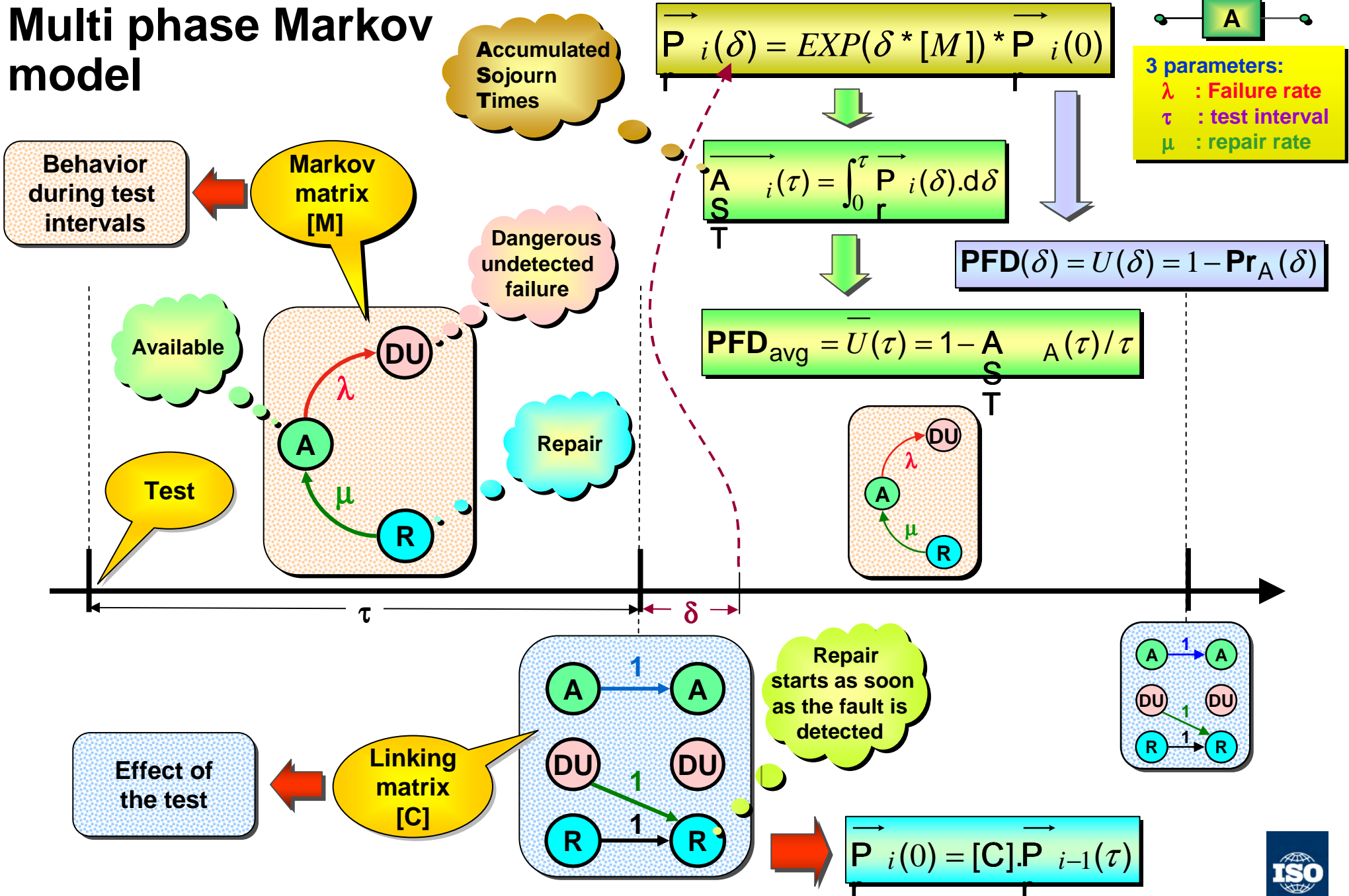
Multi-phase Markovian approach

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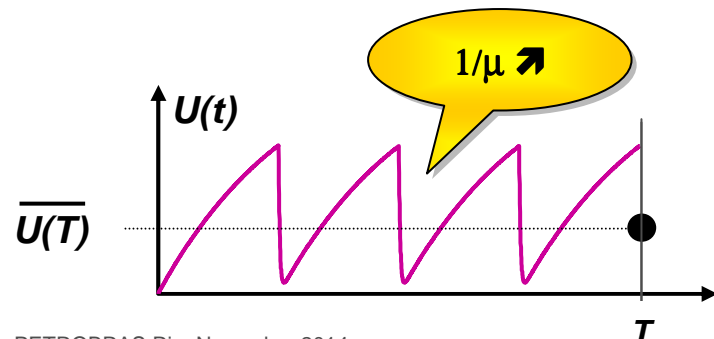
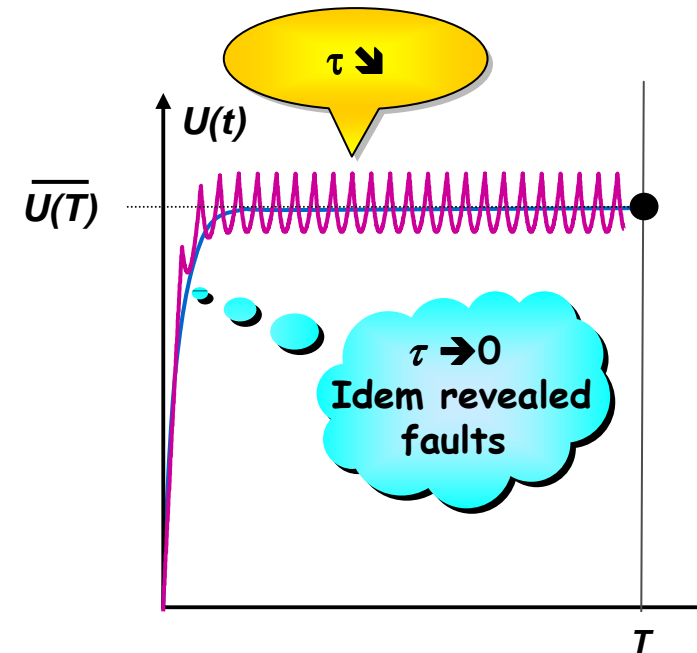
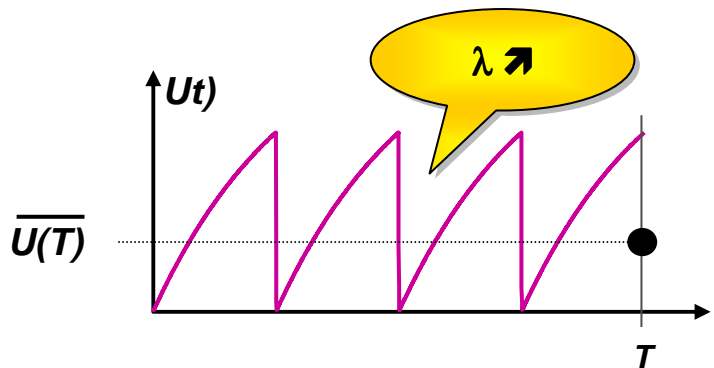
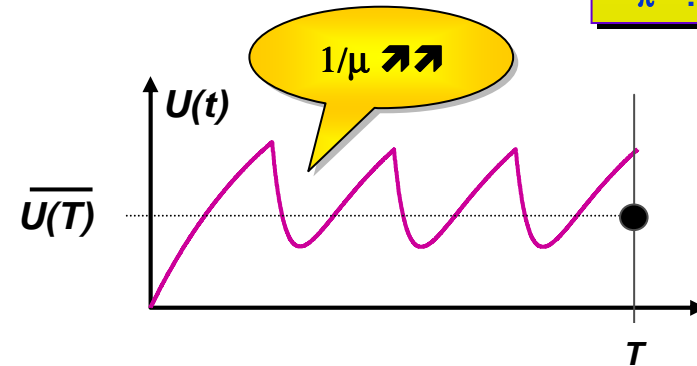
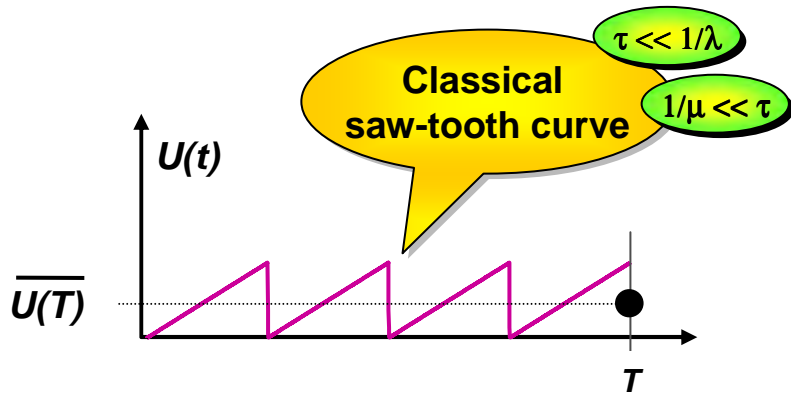
Multi phase Markov model



Typical saw-tooth curves for a single periodically tested component

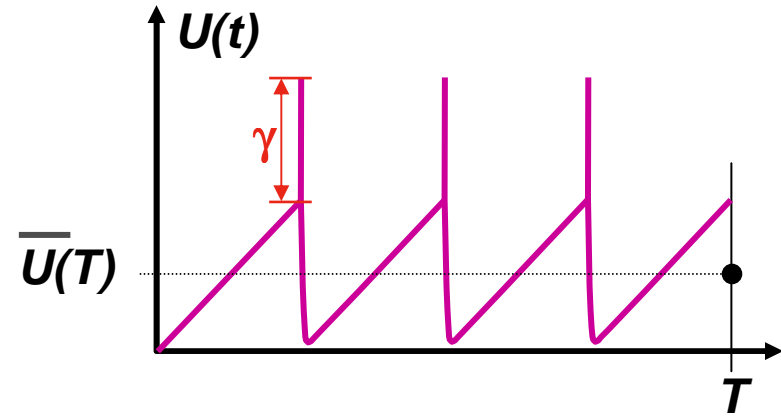
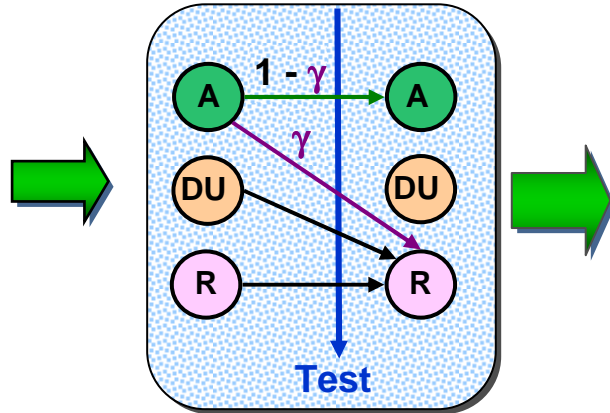


- Parameters:**
- λ : failure rate
 - τ : test interval
 - μ : repair rate
 - γ : prob. failure due to a demand
 - π : test duration

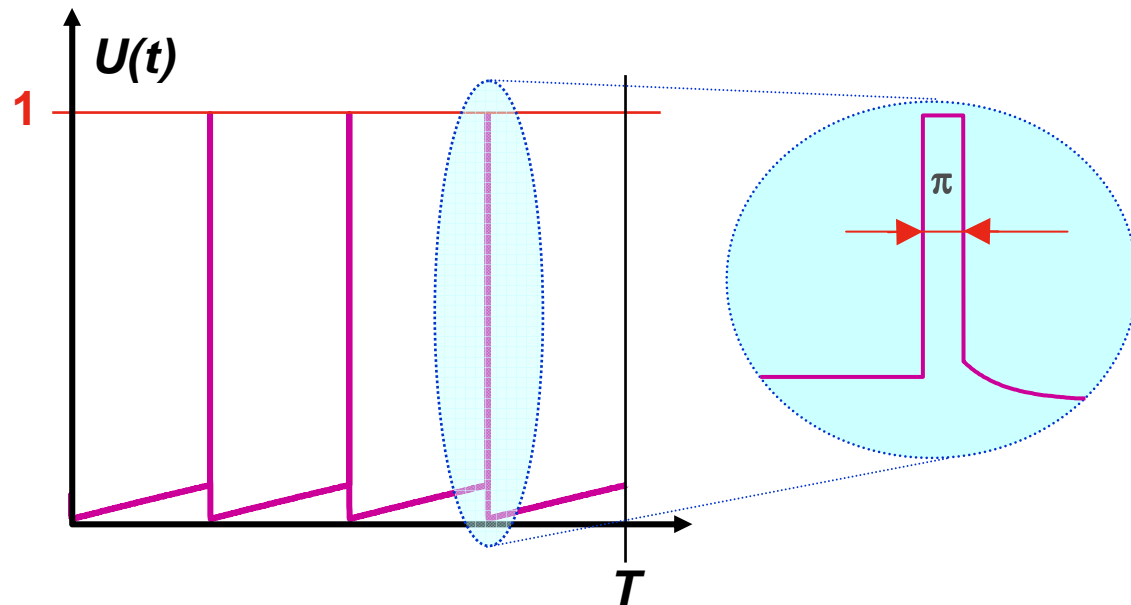
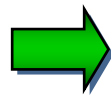


Modeling the probability of failure due to the demand itself and the test duration

Failure due to tests (γ)



Test duration



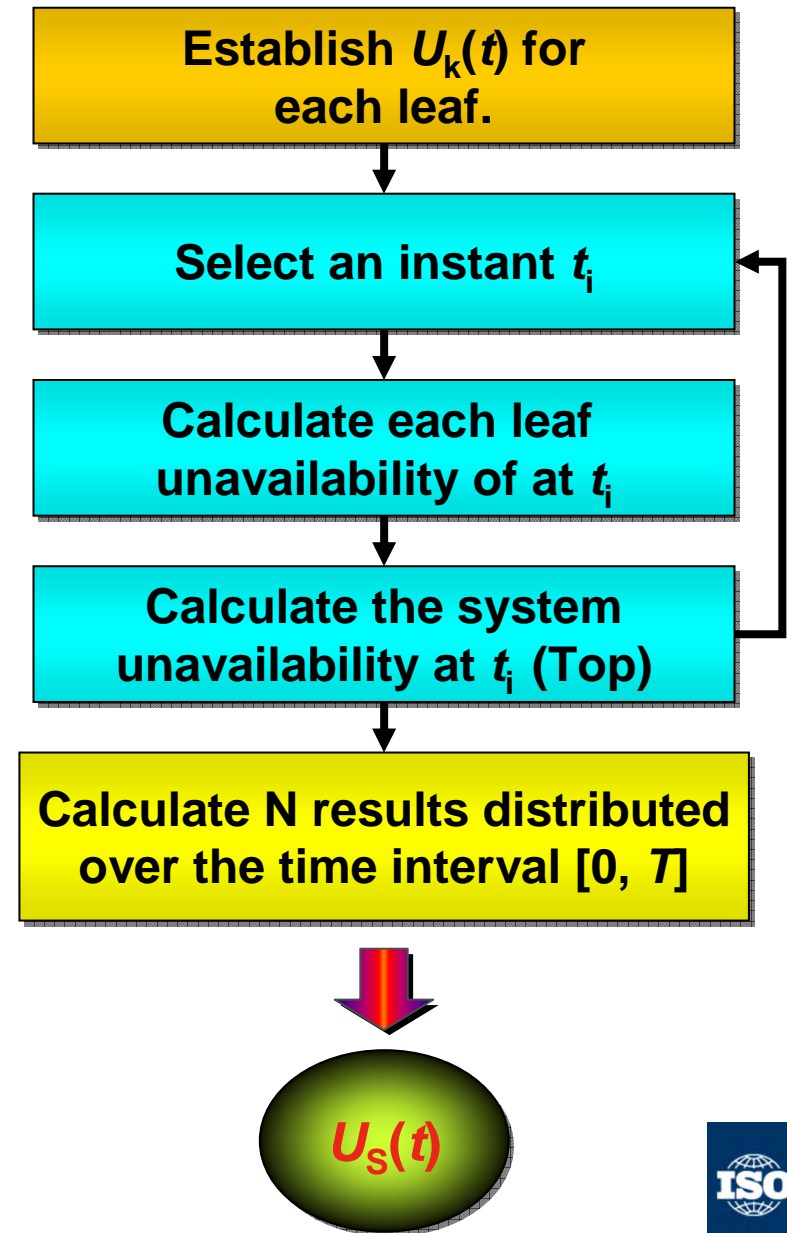
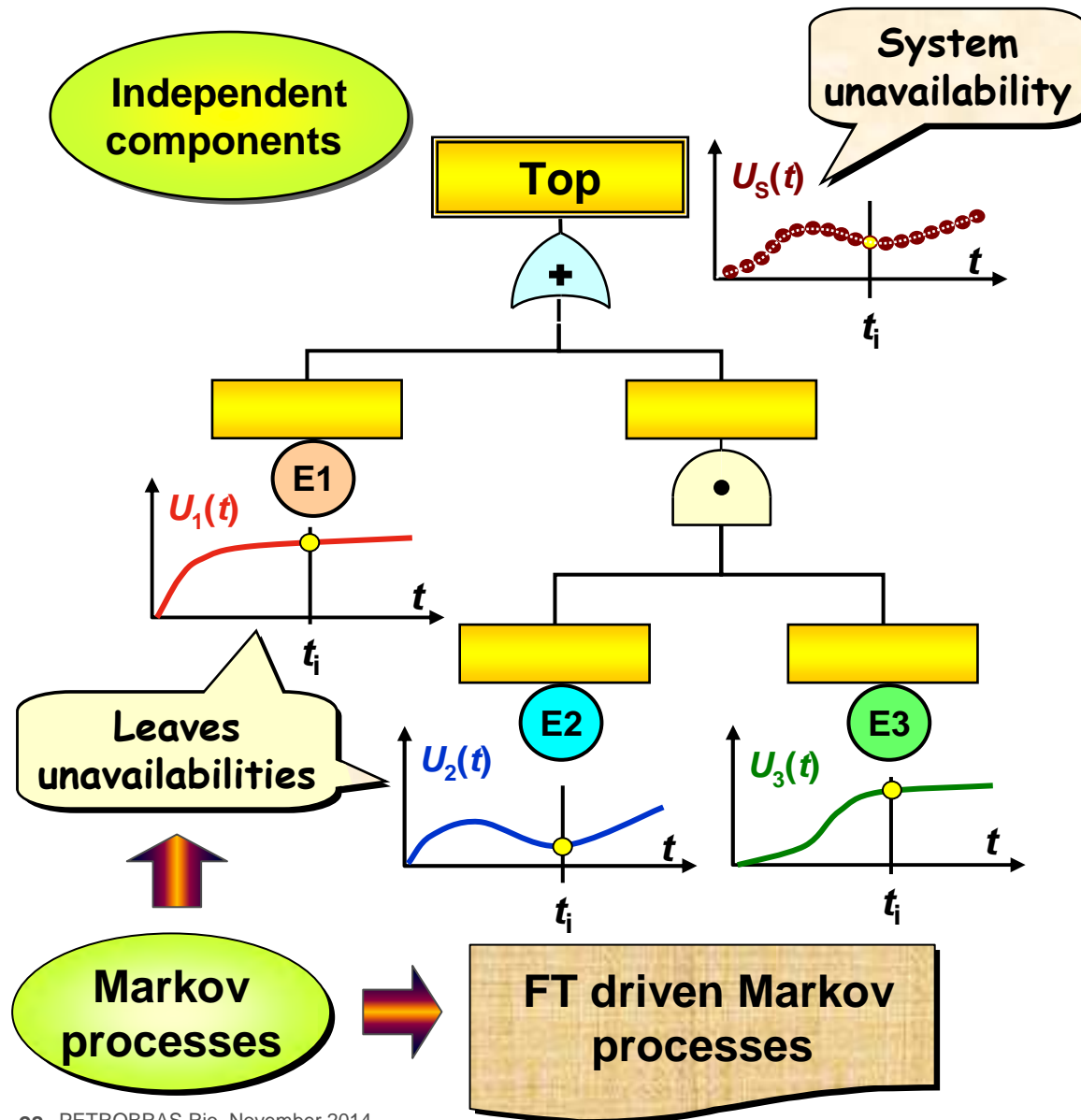
Fault tree approach

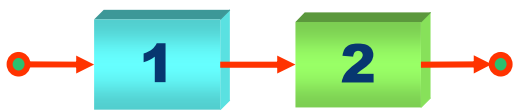
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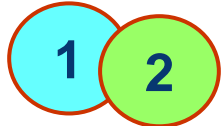
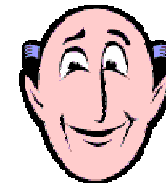
Fault tree driven Markov processes: principle for unavailability calculation.





Independent components

OR gate



Be cautious

$\lambda : 1e-4$
 $\tau : 1000$

??!

Conservative

- No Max value
- Staggering not possible

$9.75 \cdot 10^{-2}$

TOP



Usual Calculations

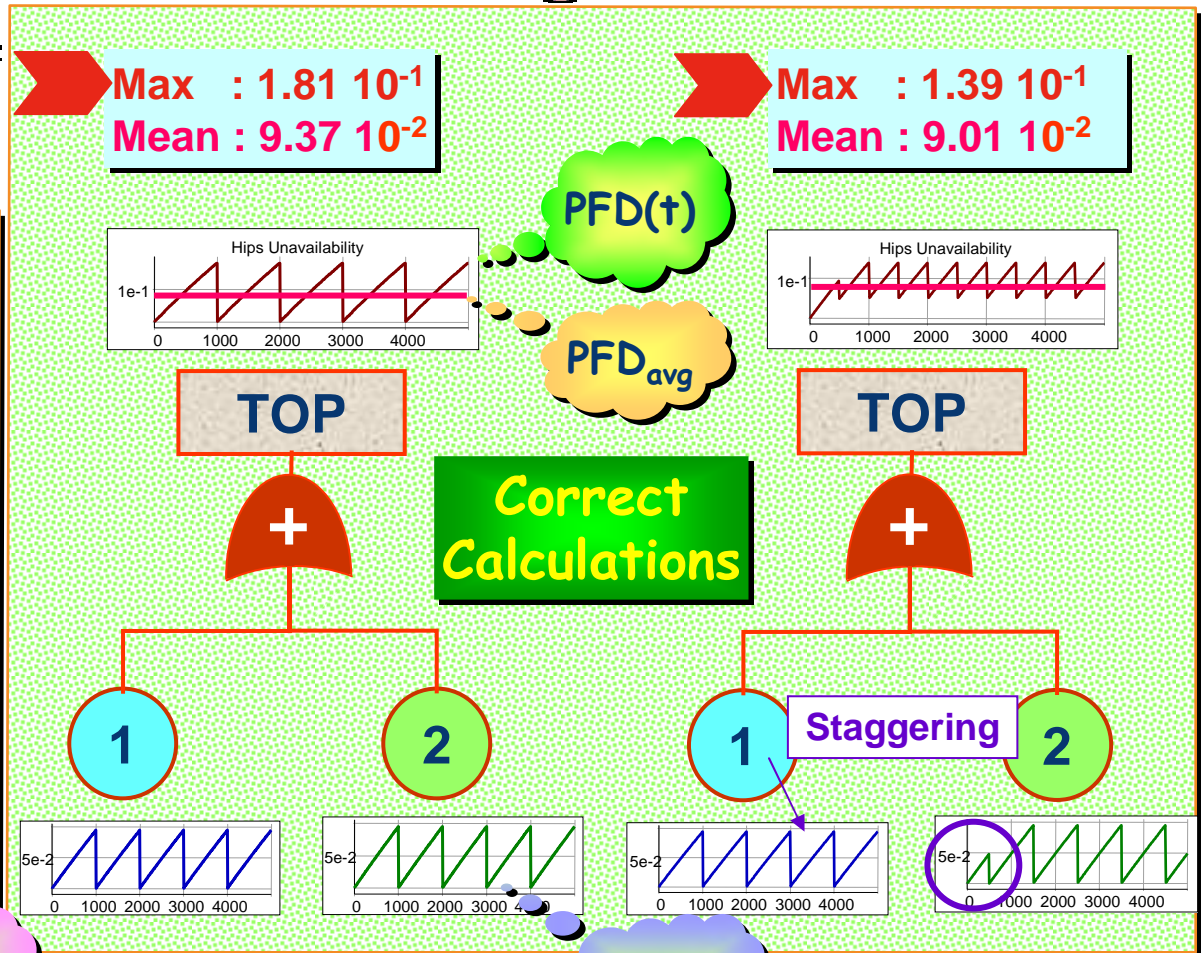


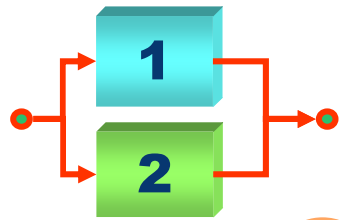
$5e-2$
 $(\lambda\tau/2)$



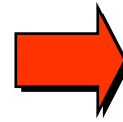
$5e-2$
 $(\lambda\tau/2)$

PFD_{avg}

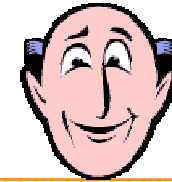




Independent components

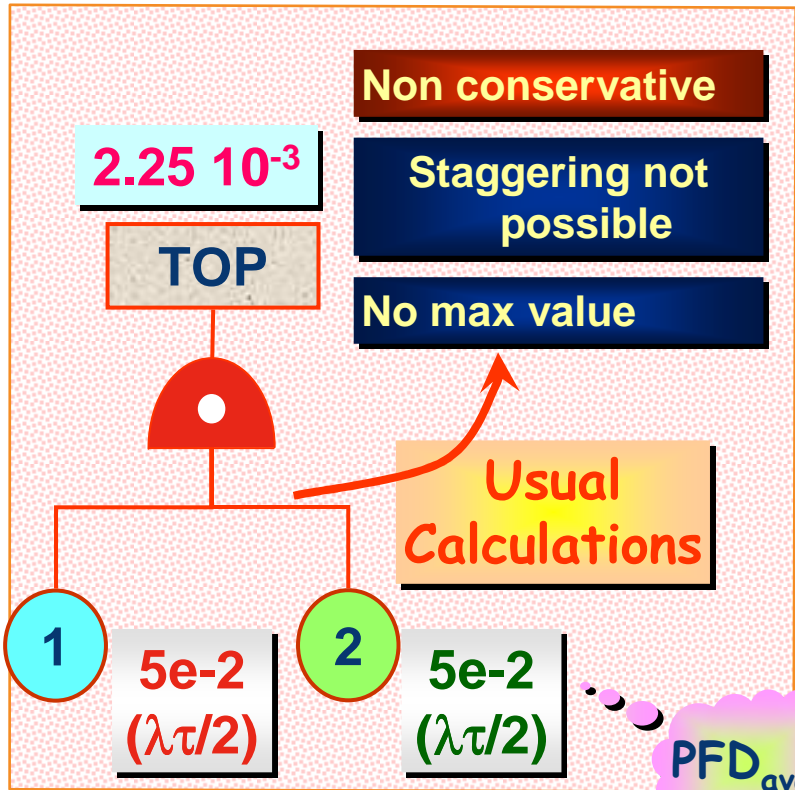
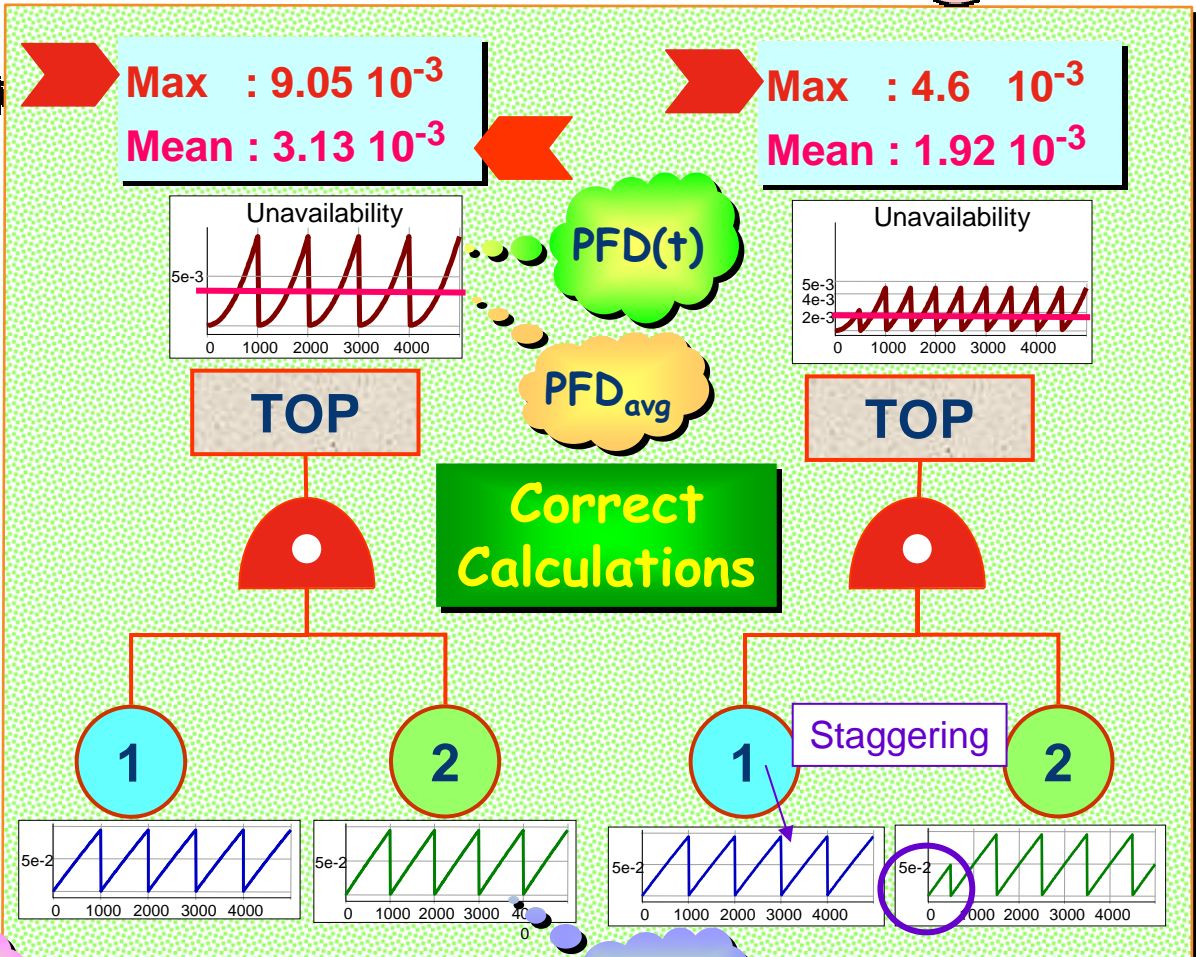


AND gate



1 2
 $\lambda : 1e-4$
 $\tau : 1000$

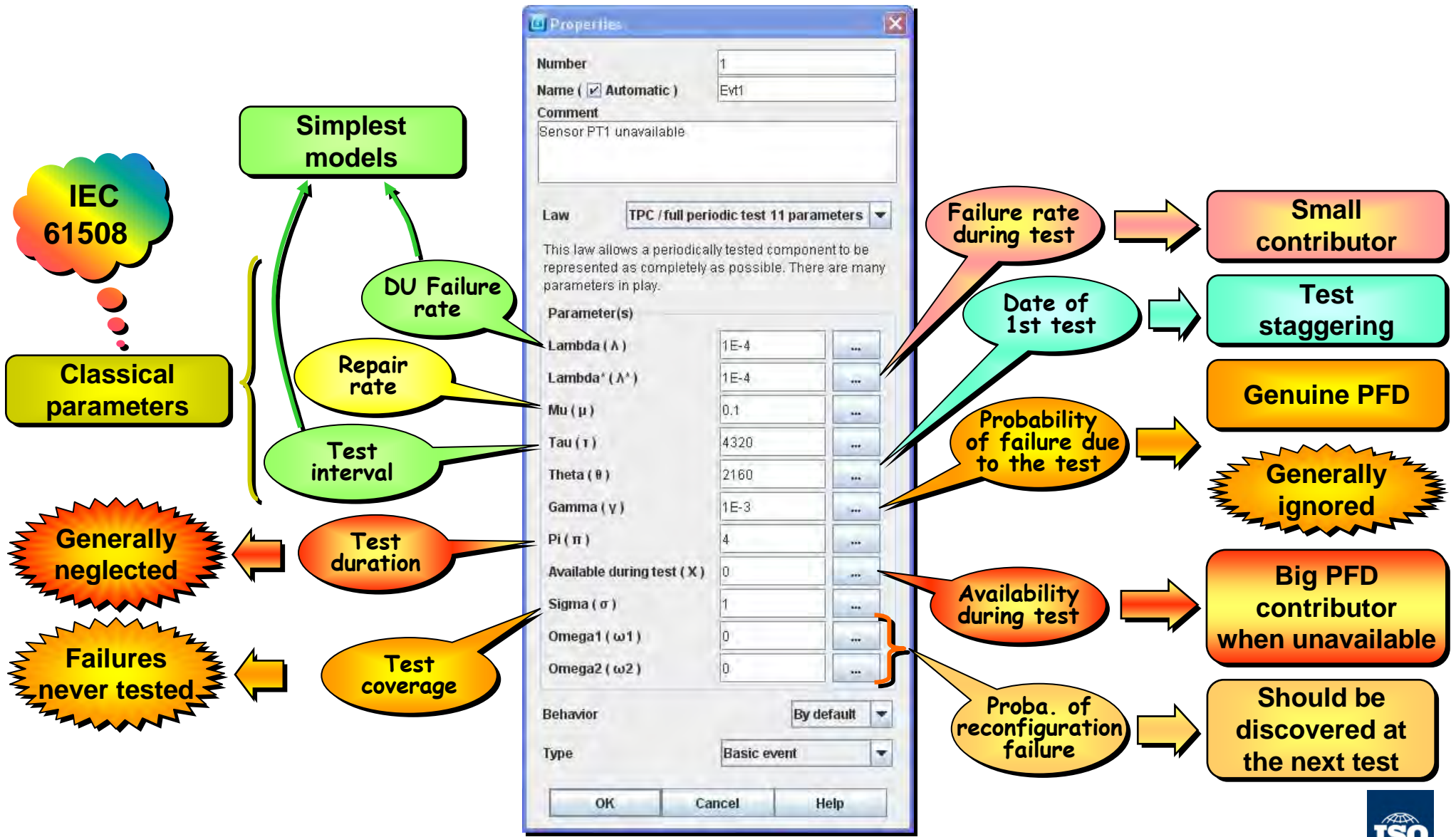
Be very cautious



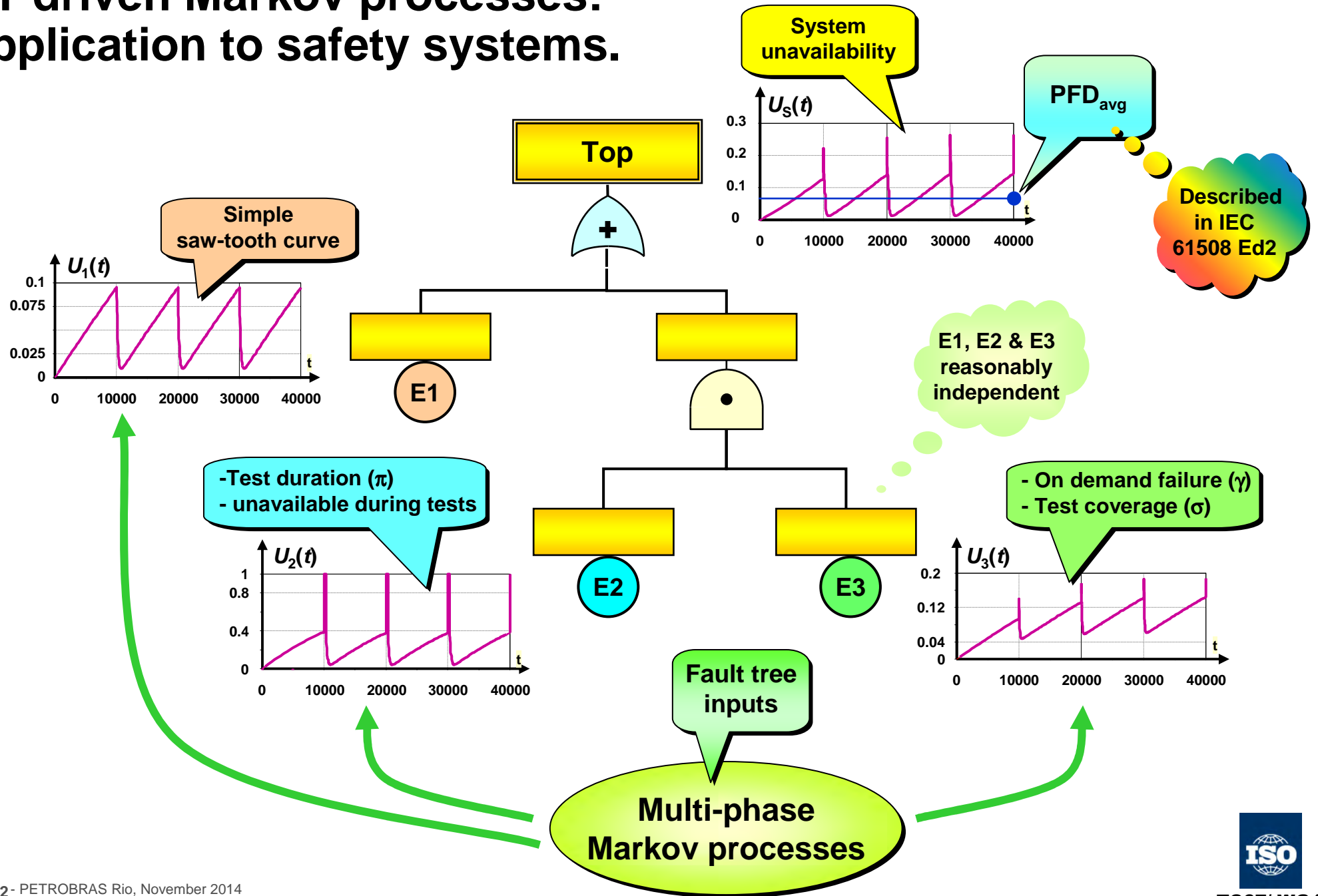
PFD_{avg}

$PFD(t)$

Parameters of a periodically tested component (dangerous undetected failures)



FT driven Markov processes: application to safety systems.



RBD driven Petri net and Monte Carlo simulation approaches

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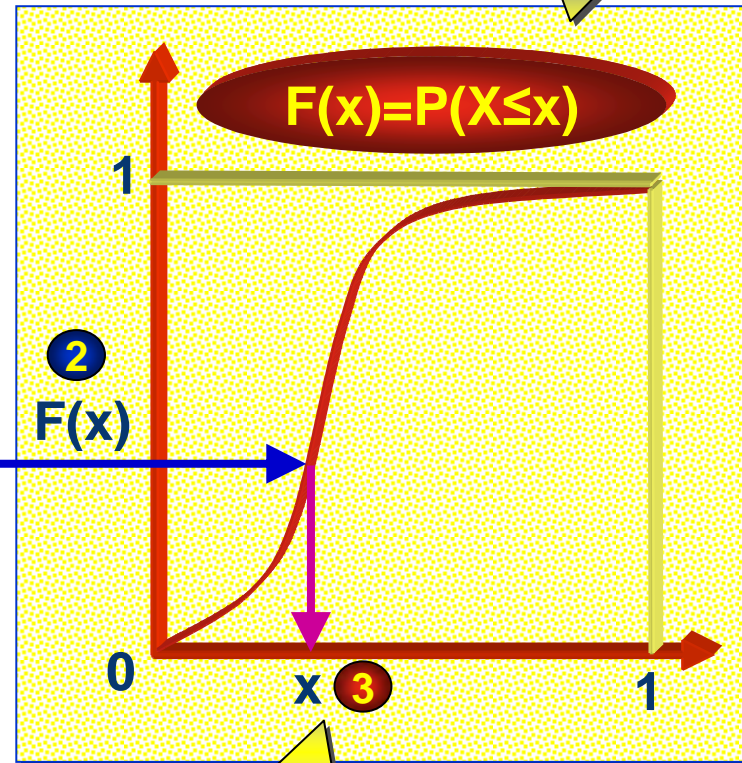
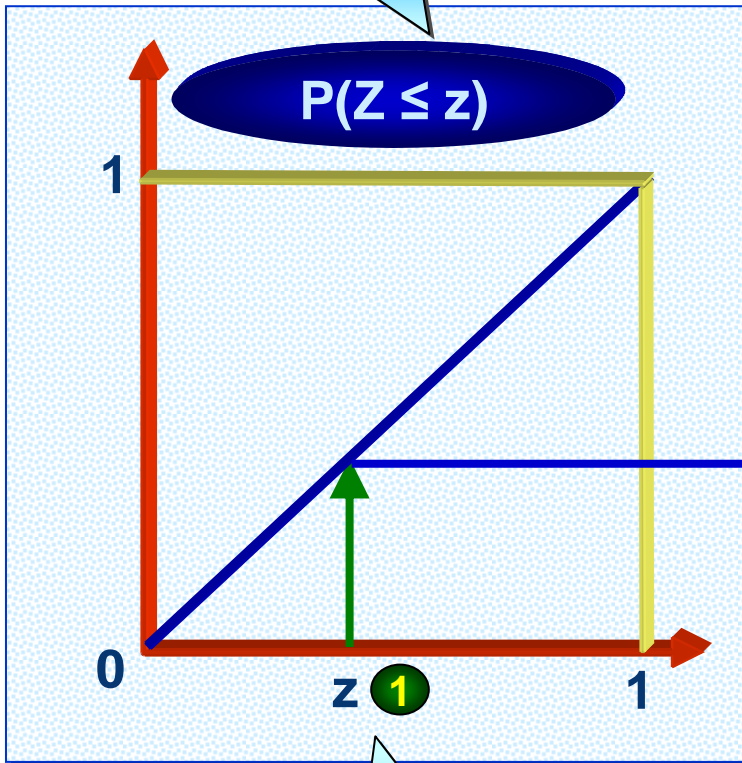


Simulation of any probability law

Z: Uniform distribution

Cumulated distribution function (cdf)

X: wanted distribution (cdf)



Random number

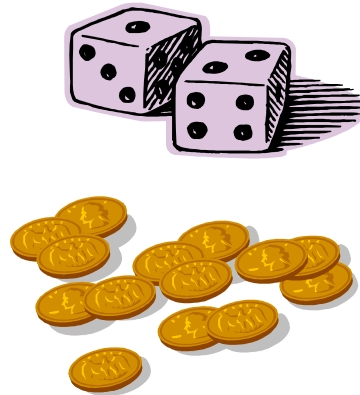
$x = F^{-1}(z)$ distributed along to $F(x)$

ex: delay δ exponentially distributed

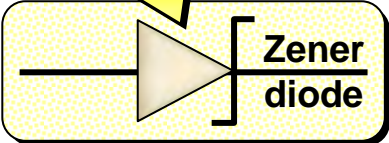
$$\delta = \frac{-LN(z)}{\lambda}$$

Random number generators

Physical methods



Thermal noise




Several billions are known

Decimals of π




3,14159265358979323846264338327950288419716939937510
58209749445923078164062862089986280348253421170679
82148086513282306647093844609550582231725359408128 ...

J. Von Neumann 

Pseudo random number generators


$X_{n+1} = (a \cdot X_n + b) \text{ mod } m$

Trajectory of the boule 

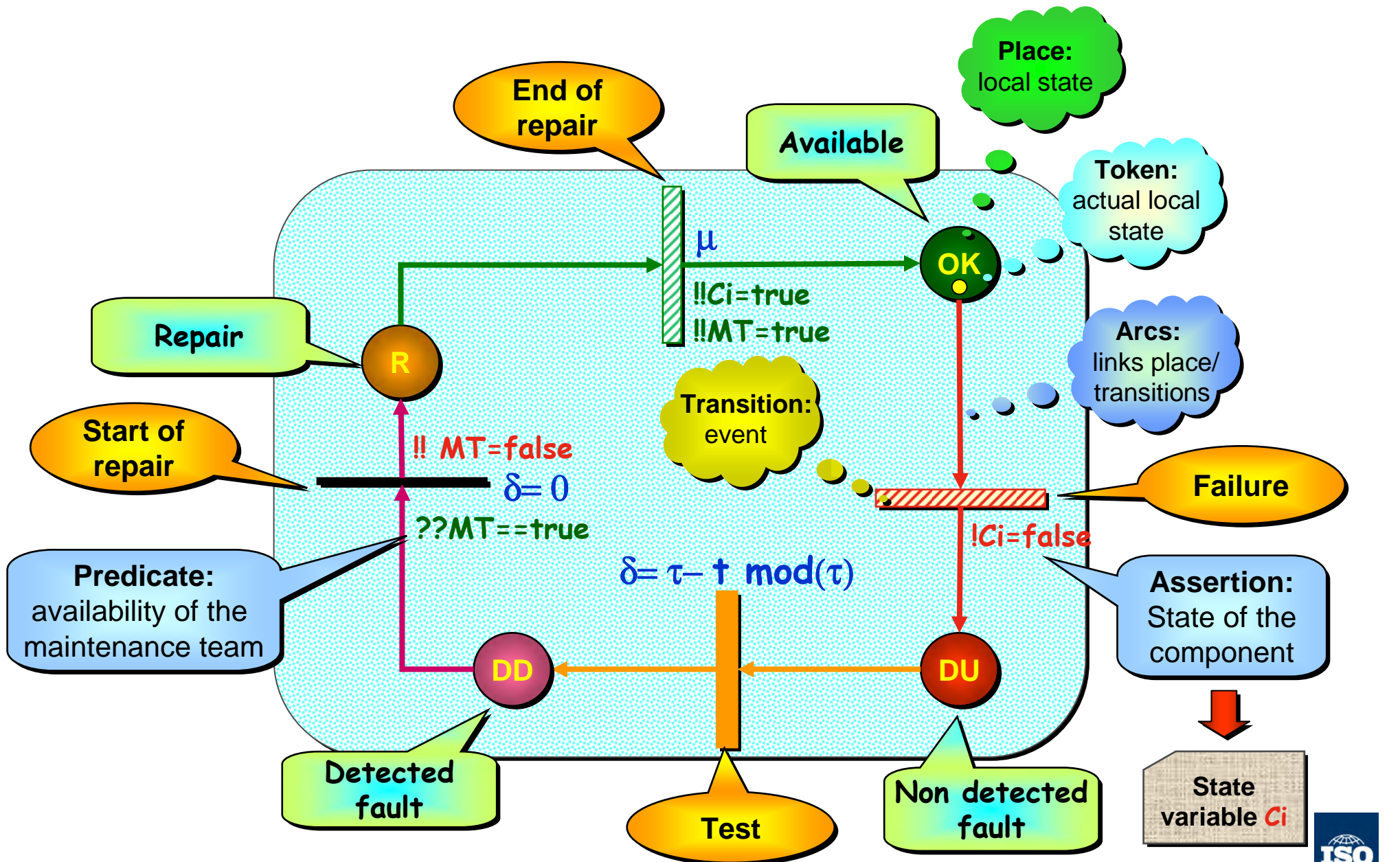
Linear congruential generators

Length of one revolution

Widely used

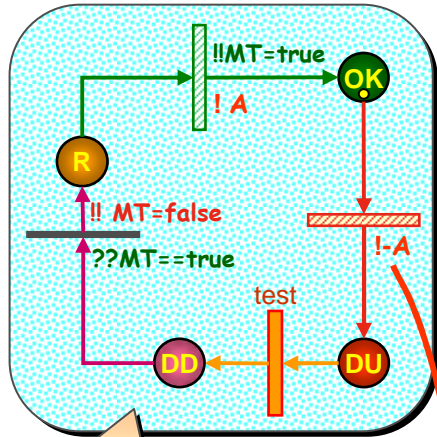
Computer 

Periodically tested component



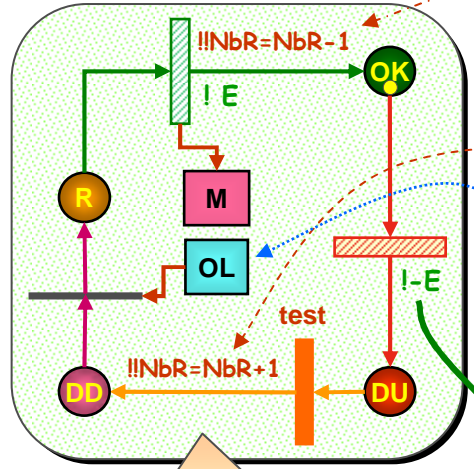
RBD driven PN modelling: application to SIL calculations

- Nb. component failed: INbR
- Repair resources on location: OL
- Repair team mobilized: M

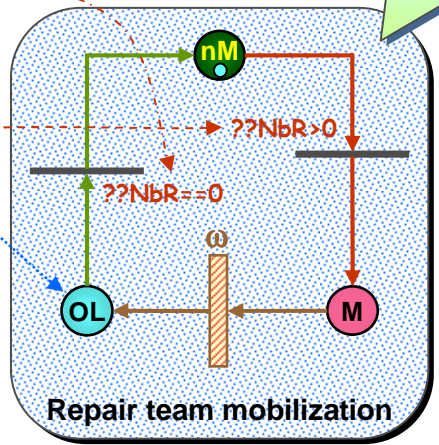


Simple periodically tested component

State variable **A**



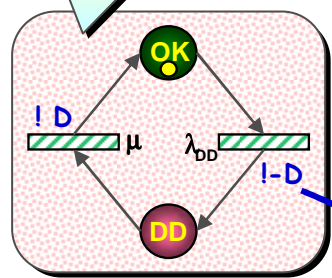
Simple periodically tested component with repair team mobilization



Repair team mobilization

State variable **E**

Simple component with revealed failures

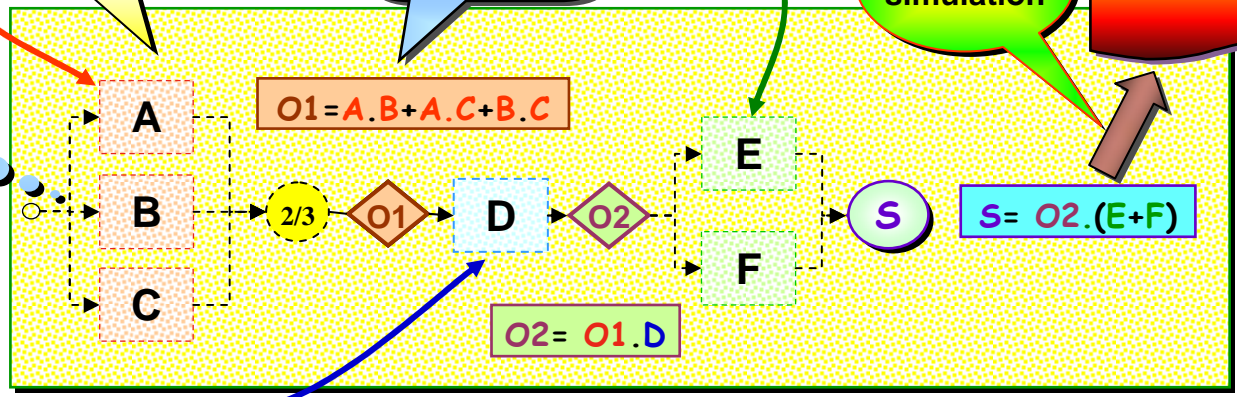


Virtual RBD

State variable **D**

SIS model

Global assertion



Monte carlo simulation

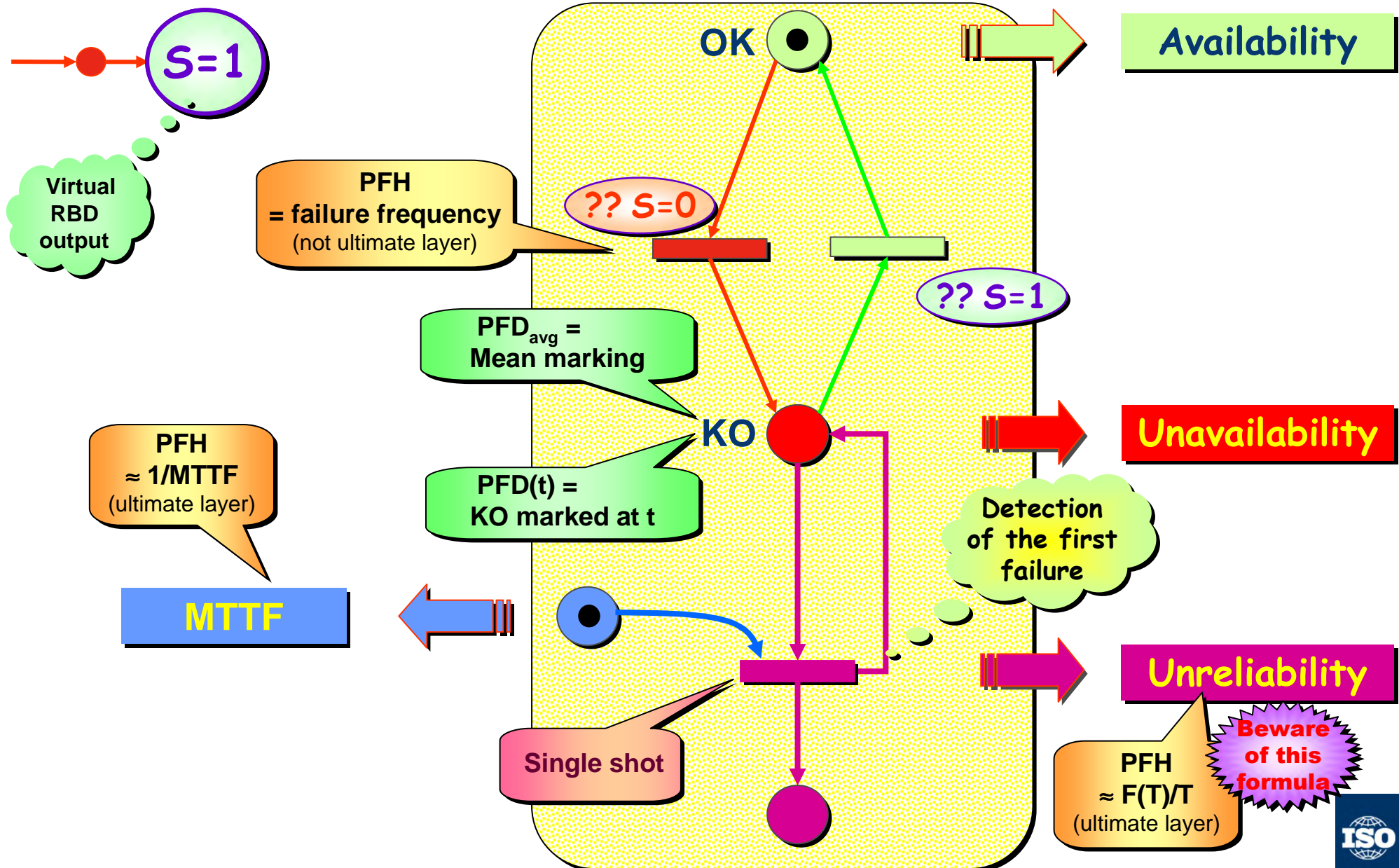
Statistics

- PFDavg
- PFH

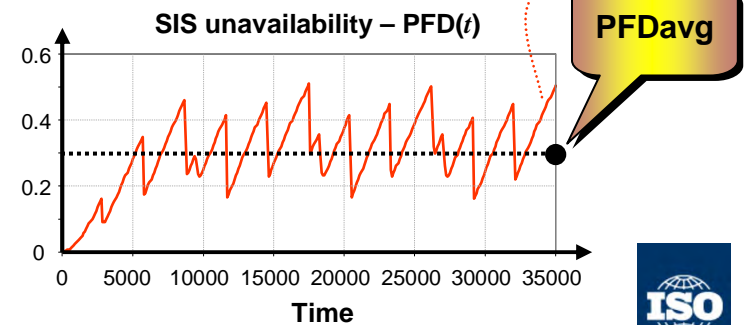
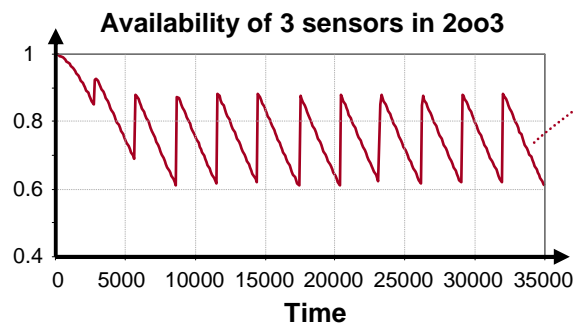
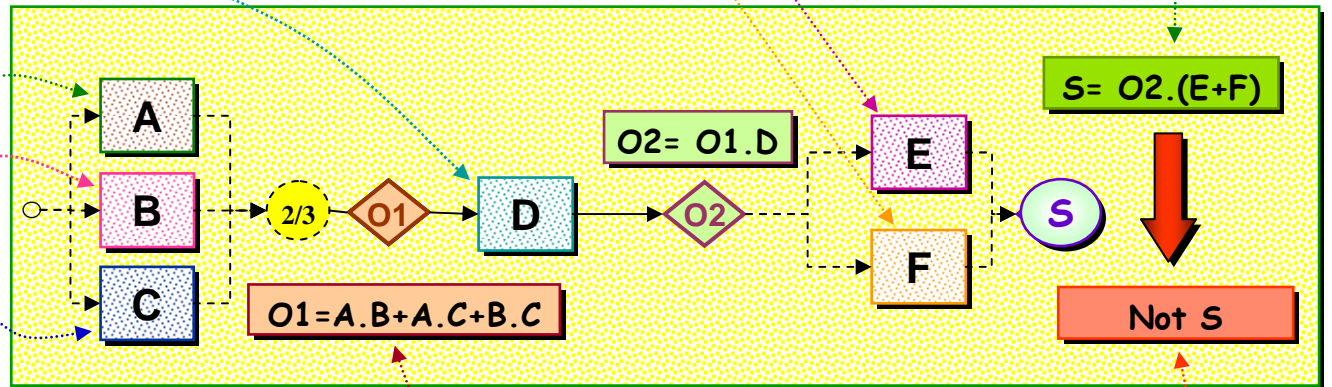
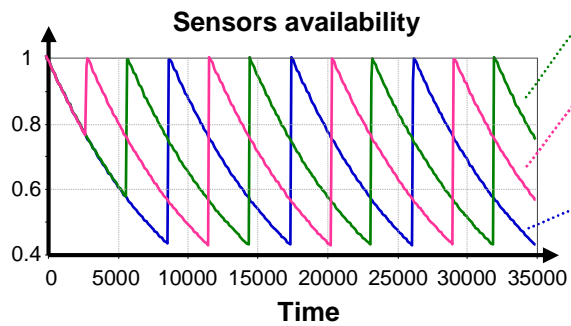
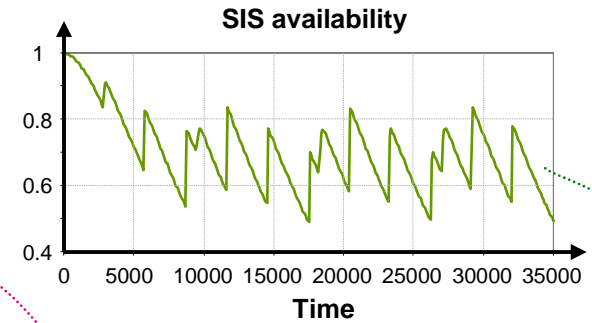
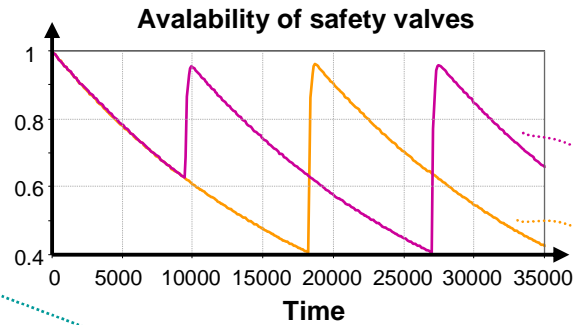
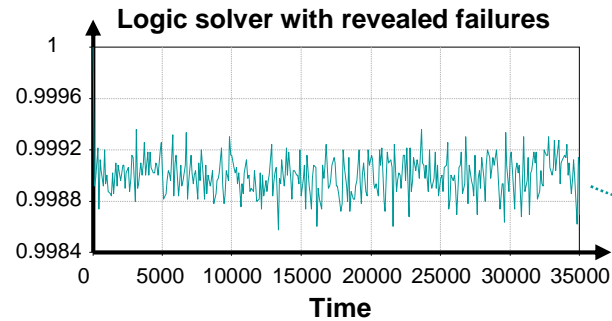
IEC 61508
ISO/TR 12489

- Reliability
- Availability
- Frequency

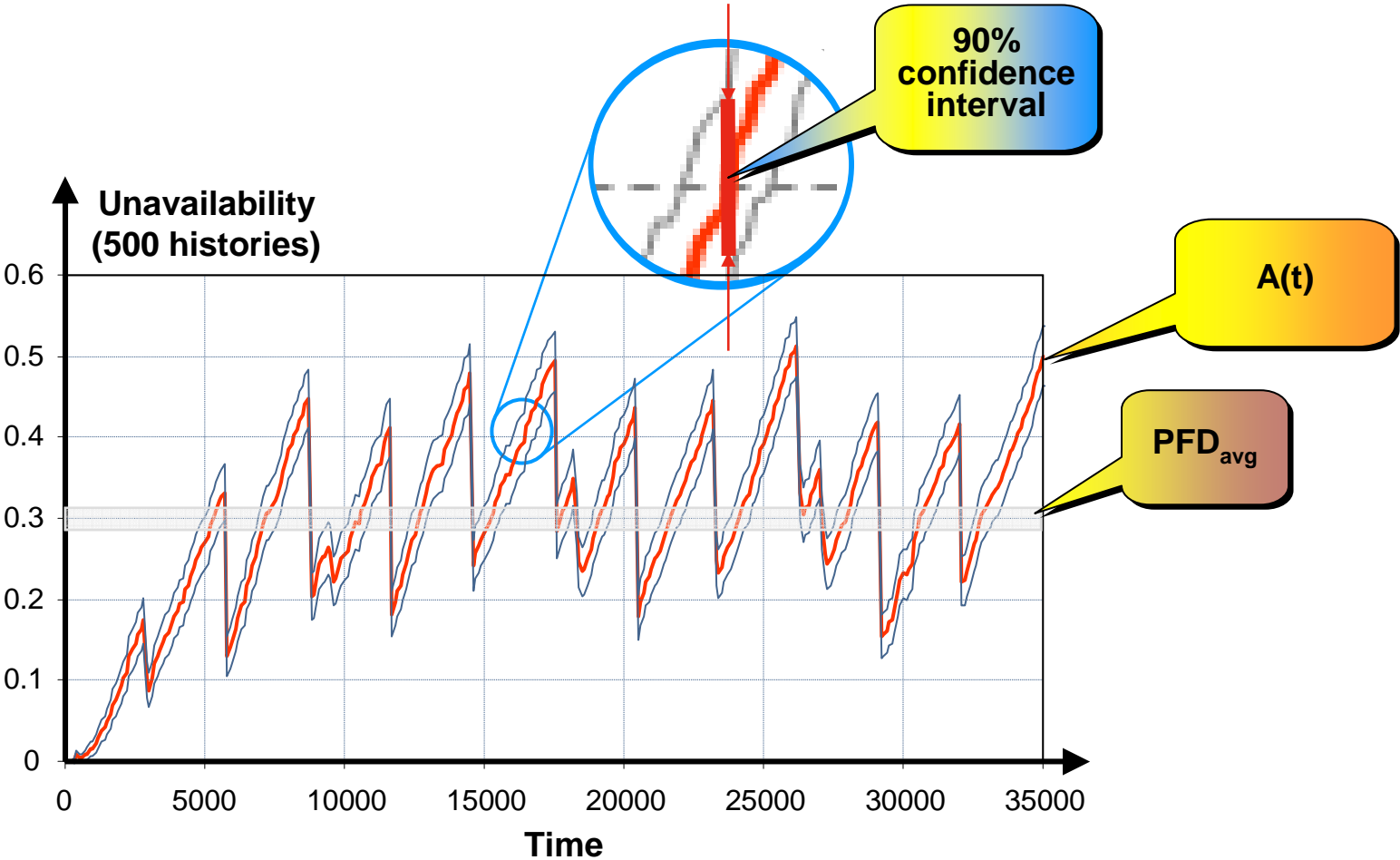
Parameter calculations: The *magic* sub PN!



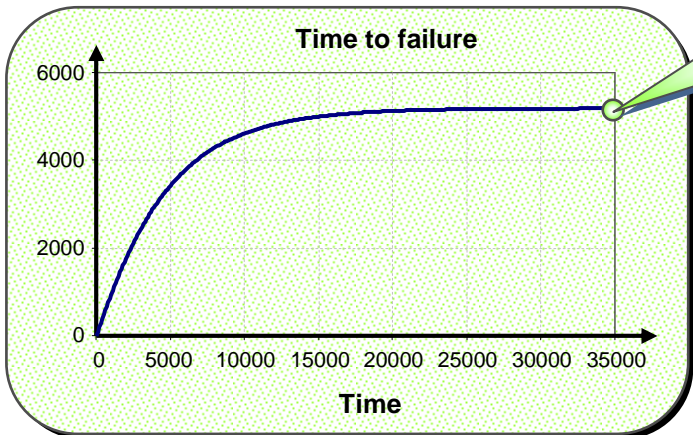
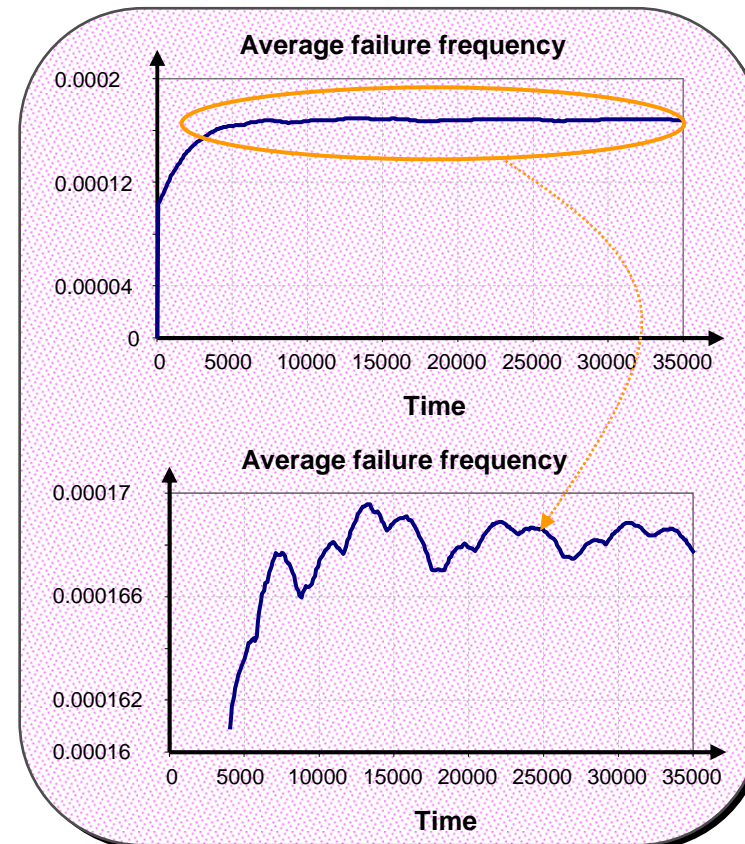
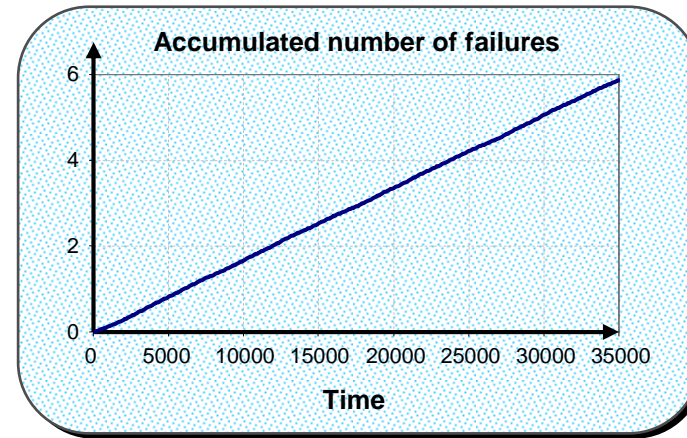
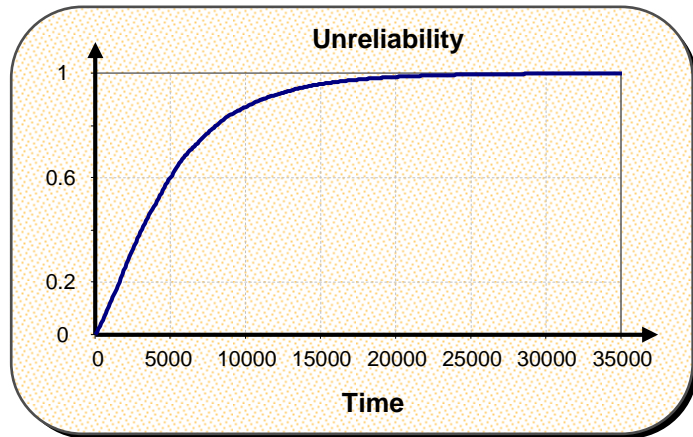
Example of Monte Carlo output (50 000 histories)



Monte Carlo simulation uncertainties



Other possible outputs



MTTF

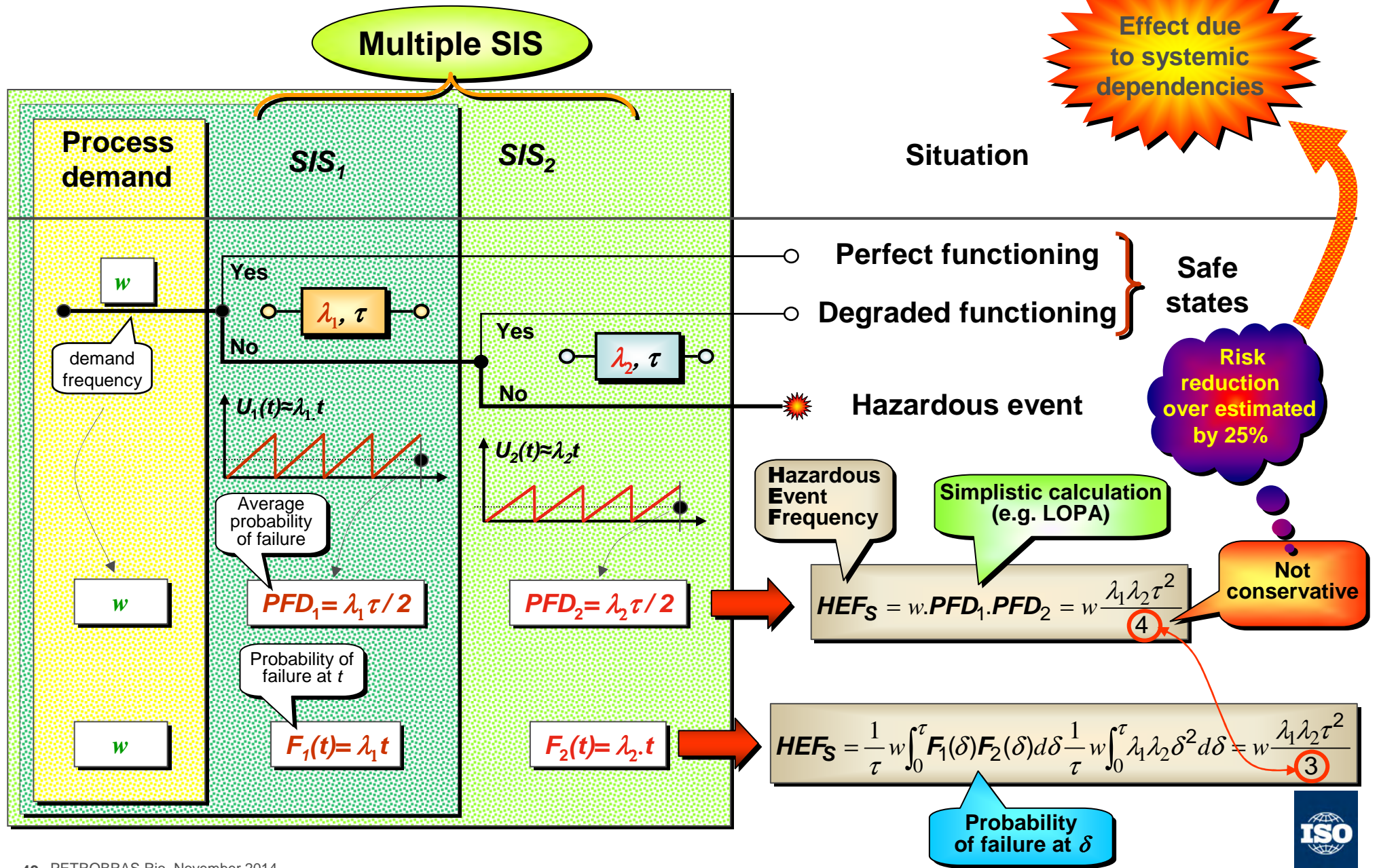
Multiple safety systems

PETROBRAS Rio, November 2014

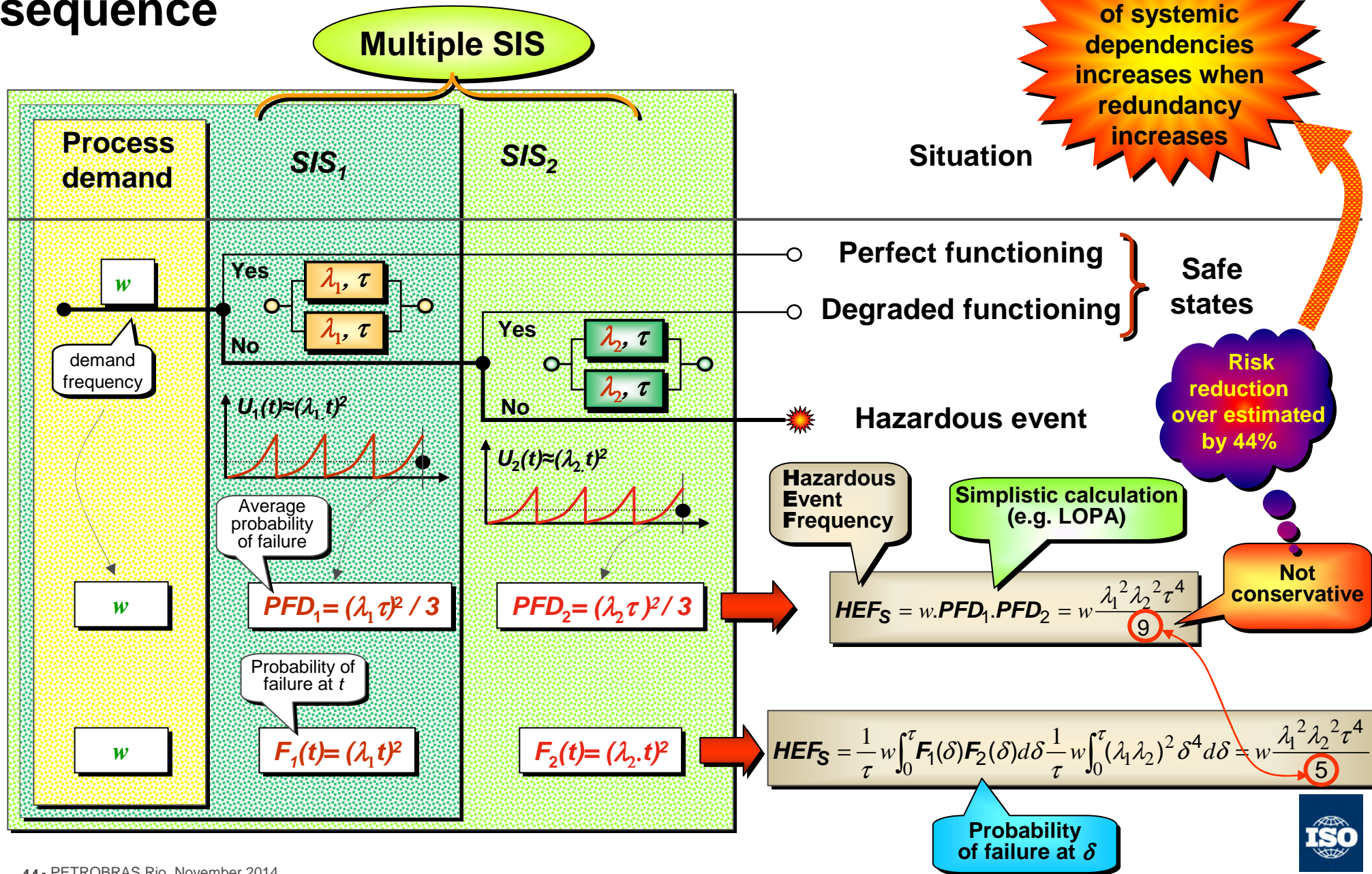
TC67
WG4



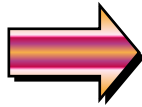
Two simple SIS acting in sequence



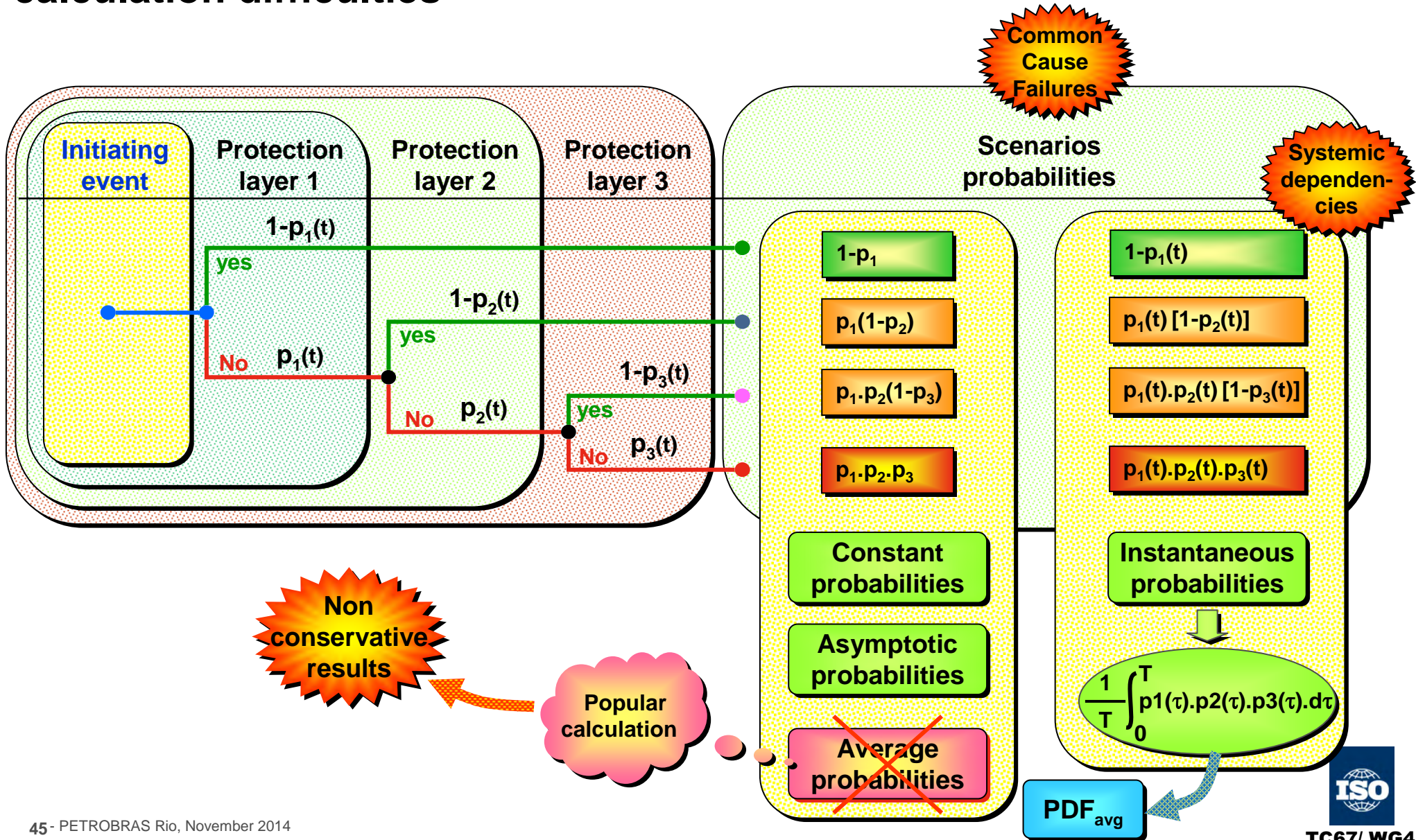
Two Redundant SIS acting in sequence



Event tree (multiple SIS) or fault tree (redundant SIS) calculation difficulties

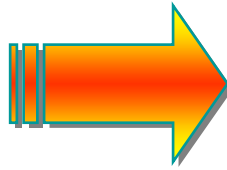


Explained in IEC 61511 and ISO/TR 12489



Any
questions
?...

SIL Bridge !



**PFDavg is not really
a good indicator for
worker in operation**

